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Silent T¹ **Mapping Using the Variable Flip Angle Method with B**¹ **Correction**

Emil Ljungberg1[∗] **| Tobias Wood¹ | Ana Beatriz Solana² | Shannon Kolind3,4,5,6 | Steven C.R. Williams¹ | Florian Wiesinger**†**1,2 | Gareth J. Barker**†**¹**

¹Department of Neuroimaging, Institute of Psychiatry, Psychology & Neuroscience, King's College London, London, UK

²ASL Europe, General Electric Healthcare, Munich, Germany

³Department of Physics and Astronomy, University of British Columbia, Vancouver Canada

⁴Department of Radiology, University of British Columbia, Vancouver, Canada

5 International Collaboration on Repair Discoveries, University of British Columbia, Vancouver, Canada

⁶Medicine (Neurology), University of British Columbia, Vancouver, Canada

†Authors contributed equally to this work

Correspondence

Emil Ljungberg, Department of Neuroimaging, Institute of Psychiatry, Psychology & Neuroscience, King's College London, London, UK Email: emil.ljungberg@kcl.ac.uk

Present address

[∗]Centre for Neuroimaging Sciences, Institute of Psychiatry (PO89), De Crespigny Park, London SE5 8AF, United Kingdom

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Purpose: To compare the silent Rotating Ultra-Fast Imaging Sequence (RUFIS) to a traditional Cartesian spoild gradientecho (SPGR) acquisition scheme for Variable Flip Angle (VFA) T_1 mapping.

Method: A two point VFA measurement was performed using RUFIS and Cartesian SPGR in a quantitative phantom and healthy volunteers. To correct for B_1 errors, a novel Silent Magnetisation Prepared B_1 map Acquisition (SIMBA) was developed, which combined with RUFIS VFA allows for a completely silent T_1 mapping protocol.

Results: The silent protocol was found to have comparable repeatability but higher reproducibility in vivo compared to the standard SPGR protocol, and showed no increase in acoustic noise levels above background noise levels compared to a 33 dBA increase for the SPGR acquisition.

Conclusion: VFA T₁ mapping using RUFIS is a feasible alternative to SPGR, achieving silent T_1 mapping with comparable acquisition time.

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K E Y W O R D S

 T_1 , Quantitative, MRI, Silent, ZTE

¹ **1** | **INTRODUCT ION**

² The variable flip angle method (VFA), also referred to as DESPOT1, is a method for T_1 estimation, originally proposed $\,$ by Christensen and later adapted for imaging by Fram [1, 2, 3, 4, 5]. To obtain a T₁ estimate, two or more fully spoiled ⁴ gradient echo images are acquired with varying excitation flip angles and linearly fitted to the signal equation [6]. Due to the use of a gradient-echo sequence and the low number of acquisitions required, the VFA method is highly efficient compared to inversion-recovery based methods [7]. However, due to the large phase-encoding and spoiler gradients and short TR typically used in clinical protocols, the VFA method produces loud acoustic noise which is a drawback for patient comfort. In addition, at modern field strengths of 3T and above, B_1 inhomogeneity becomes a significant issue that must be corrected for with a separate acquisition. ¹⁰ In this work, we present a method for VFA T¹ mapping using the 3D **R**otating **U**ltra-**F**ast **I**maging **S**equence $_{11}$ (RUFIS)[8], which presents several potential advantages over a traditional Cartesian acquisition. First, because of

¹² the centre-out radial *k*-space trajectory and gradual change of the gradient direction between subsequent excitations, ¹³ the acquisition is almost completely silent [9]. Secondly, the RUFIS sequence achieves an effective echo time of zero 14 (ZTE) by performing RF excitation with the readout gradients on and directly acquiring the free induction decay (FID)[10]. ¹⁵ This extends the limit of T₁ quantification to tissues with very short T₂ such as bone and lung tissue, which often are 16 considered to be MR-invisible $[11, 12]$.

¹⁷ We present theoretical signal equations for RUFIS and analyse the constraints imposed on the acquisition by the ZTE readout. The theory and implementation of a novel silent B_1^+ mapping technique, using an extension to the double angle method with a RUFIS readout, is also presented. The proposed silent T_1 and B⁺ mapping techniques are ²⁰ demonstrated in a quantitative phantom with known relaxation characteristics and in vivo in four healthy volunteers, 21 and compared to Cartesian methods.

²² **2** | **METHOD**

²³ **2.1** | **Theory - Quantitative RUFIS**

 $_{24}$ An outline of the RUFIS pulse sequence diagram is shown in figure 1A. Each spoke is a single FID readout with a centre- 25 out trajectory in k-space. The magnitude of the applied gradients remains the same, while the relative strength along ²⁶ each axis changes the direction of the spoke in k-space. The k-space trajectory is designed such that the endpoints of 27 the spokes trace a spiral on the surface of a sphere in k-space, resulting in a near silent acquisition [9]. Data acquisition 28 starts as soon as the system has switched from transmit to receive mode, resulting in an effective echo time of zero 29 (ZTE). To achieve this, only ultra-short hard RF pulses with low flip angles can be used for excitation with RUFIS. Further ³⁰ more, the TR in RUFIS is only limited by the readout duration since no time is required for slice/slab and phase encoding 31 gradients.

³² When a steady state has been reached with RUFIS, the acquired signal will be equivalent to that of a spoiled gradient 33 echo sequence, with the signal intensity depending on T_1 and proton density ρ , as well as the repetition time (TR), and 34 flip angle (α) as

$$
M_{z,spgr} = \rho \cdot \frac{1 - e^{-TR/T_1}}{1 - \cos(\alpha)e^{-TR/T_1}}.
$$
 (1)

³⁵ With RUFIS, only short TRs and low flip angles are used, and therefore a first order approximation of (1) can be

³⁶ made [13, 14] as

$$
M_{z,spgr} = \frac{\rho}{1 + \frac{T_1}{TR} \cdot \frac{\alpha^2}{2}}.
$$
 (2)

37 This assumes that the signal is fully spoiled between repetitions. In RUFIS, this is achieved with RF spoiling as well as 38 gradient spoiling from the readout gradients.

39 To perform a T₁ measurement using the variable flip angle method (VFA), a minimum of two flip angles is required. ₄₀ Spatial variations in the B $_1^+$ field have to be measured independently since changes in T₁ and α cannot be separated $_{41}$ in the signal equation, as seen in (2). In RUFIS, there are two sources of B_1^+ variation; dielectric effects, and excitation ⁴² profile effects. The former is here addressed through development of a novel B⁺ mapping technique using RUFIS 43 (described in the next section), and the latter through an analytical correction.

⁴⁴ The non-uniform excitation profile in RUFIS is caused by the readout gradient being present during RF excitation[15]. ⁴⁵ For a given spoke, the gradients alter the resonant frequency across the sample parallel to the spoke direction, resulting in an unwanted sinc-shaped spatial variation of the flip angle in the direction of the spoke. The excitation profile is 47 determined by the product of the duration of the RF pulse (τ_{rf}) and readout gradient magnitude G (which is inversely 48 proportional to the readout bandwidth) as

$$
B_1^+(\bar{r}) = \text{sinc}(\tau_{rf} \cdot \omega_G) \tag{3}
$$

where $\omega_G = \gamma \cdot \bar{G} \cdot \bar{r}$, γ is the gyromagnetic ratio, and \bar{G} and \bar{r} are vectors describing the current gradient direction and 50 the position in the sample, and max $|\omega_G| = rBW$, i.e. the readout bandwidth.

⁵¹ In order to achieve a flat excitation profile, hard RF pulses with the shortest possible duration should be used. This 52 requires using the maximum possible RF amplitude and choosing the duration of the RF pulse to be that required to ₅₃ achieve the highest flip angle desired. This introduces a practical upper limit of the maximum flip angle that can be 54 achieved. Therefore, optimization of a RUFIS VFA T₁-mapping protocol has to consider a series of linked constraints. ⁵⁵ First, given a readout bandwidth the maximum excitation pulse width is limited to maintain an acceptable excitation ₅₆ profile; here we chose a limit of τ_{rf} · r BW < 0.5 which results in the excitation flip angle at the edge of the FoV falling
₅₇ to 63% of the prescribed flip angle. The chosen bandwidth will also determine the T to 63% of the prescribed flip angle. The chosen bandwidth will also determine the TR. The optimal flip angle sampling 58 scheme in a VFA acquisition depends on the TR of the acquisition and the T₁ for which it is optimised [16]. With T₁ ⁵⁹ fixed, the optimal flip angles decrease with shorter TR. At the same time, a shorter TR, resulting from higher bandwidth, ⁶⁰ will also result in a shorter pulse width, and thus lower achievable flip angles. Tests on our scanner revealed that the ⁶¹ pulse-width is the main limiting factor, and only at low bandwidths, here \pm 7.8 kHz can flip angles close to the optimal
⁶² be achieved. However, the flip angle limitations might be different for different MR sy be achieved. However, the flip angle limitations might be different for different MR systems as they depend on the RF ⁶³ amplifier, coils and SAR constraints.

2.2 | **Theory - B**⁺ ⁶⁴ ¹ **mapping with RUFIS**

 ϵ ₅₅ The proposed B₁⁺ mapping method uses a composite preparation pulse with different flip angles prior to a RUFIS readout ⁶⁶ to saturate the magnetisation proportional to the total flip angle, see figure 1B. We hereafter refer to this technique σ as SIMBA (**Si**lent Magnetisation prepared B_1^+ Acquisition). To enable magnetisation preparation, the RUFIS readout is ⁶⁸ divided into segments with N spokes per segment. A series of n RF pulses with the same phase, flip angle α_{SAT} , and ϵ_{θ} short inter-pulse spacing are applied as a preparation, acting as one composite pulse with effective flip angle $n \cdot \alpha_{SAT}$. σ The transverse magnetisation after preparation is spoiled using a spoiling gradient, resulting in an initial longitudinal

FIGURE 1 (A) Schematic pulse sequence diagram of the RUFIS sequence. Excitation is performed with an ultra-short hard RF pulse with the gradients on, and the free induction decay (FID) is acquired. The gradient magnitude stays the same and only the direction changes for each spoke. **(B)** Schematic of the SIMBA pulse sequence with the magnetisation preparation module before the RUFIS readout segment. A series of hard pulses with flip angle α_{SAT} is applied and the transverse magnetisation after the train of pulses is crushed with a gradient on the z axis. The delay τ_r between preparations allows for T_1 recovery.

 π_1 magnetisation before readout given by $\tilde{M_0}=\rho\cdot\cos(n\alpha_{SAT})$. To produce a B_1^+ mapping technique that is consistent

 72 with the RUFIS readout, ultra-short RF pulses are used in the preparation. Using similar pulses in the preparation as in

 73 the readout enables characterization of potential errors in the hard RF pulses, e.g. not reaching the peak amplitude

instantaneously, as would be the case for a perfect rectangular pulse, which would result in a global, non-spatial, B_1^+ 74

⁷⁵ error.

The observed magnetisation in a RUFIS acquisition is proportional to the average magnetisation within a segment $\bar{M_T}(N)$ which can be expressed as

$$
\bar{M}_T = \sin \alpha \cdot \bar{M}_z \tag{4}
$$

$$
\bar{M}_z = \tilde{M}_0 \cdot f + M_{z, spgr}(1 - f) \tag{5}
$$

$$
f = \frac{1 - \xi^N}{N(1 - \xi)}, \quad \xi = \cos \alpha \cdot e^{-TR/T_1}.
$$

 δ where \tilde{M}_0 is the prepared longitudinal magnetisation at the beginning of the segment, and α is the excitation flip angle

 $_{77}$ in the RUFIS readout. The full derivation of this expression can be found in the appendix. Encoding the B $^+_1$ efficiency as a

 78 factor λ , makes the transverse magnetisation proportional to λ as

$$
\bar{M}_T = \left[\rho \cdot \cos(n \cdot \lambda \cdot \alpha_{SAT}) \cdot f + M_{z,spgr}(1-f) \right] \cdot \sin \alpha \tag{7}
$$

 $\frac{1}{79}$ assuming full T₁ recovery between preparations. Figure 2A shows how the prepared magnetisation changes with the

80 total preparation flip angle $(n \cdot \alpha_{SAT})$ for $\lambda = (0.8, 1.0, 1.2)$. The repeated excitation in the RUFIS readout results in a

81 positive offset in the signal, explained by the second term in (7), as shown in figure 2B. While increasing the number of

82 spokes per segment will reduce the acquisition time, it will also reduce the dynamic range of the measurement.

FIGURE 2 (A) Simulation showing the effect of B_1^+ efficiency (λ) on the prepared magnetisation. (B) Simulation showing the effect of the RUFIS readout on the prepared magnetisation assuming $\lambda = 1$, $T_1 = 1$ s, RUFIS $\alpha = 2^\circ$ and TR=1 ms.

⁸³ **2.3** | **MR Acquisition**

84 MR experiments were performed on a GE MR750 3T scanner (GE Healthcare, Chicago, IL) using the body coil for RF $\frac{1}{85}$ transmission and a 12-channel head RF receive coil. VFA T₁-mapping data were acquired with a 3D RUFIS sequence and $_{\rm ss}$ $\;$ a Cartesian SPGR sequence for comparison. The acquisitions were matched in field of view (FOV) (192x192x192 mm 3), $_{\rm s7}$ voxel size (1.5x1.5x1.5 mm 3) and acquisition time. Because of the difference in TR between RUFIS and SPGR, a different ss set of flip angles (α) were acquired, to match the optimal set [16]. RUFIS data were acquired with α=2° & 12°, TR=4.4 ₈₉ ms, TE=0 ms, readout bandwidth=±7.8 kHz, 24576 readout spokes in total, RF spoiling phase increment=117.0°. The RF ⁹⁰ pulse width was fixed to 64 μ s. The current implementation of the RUFIS sequence is restricted to a segmented readout 91 to allow for magnetisation preparation such as T₁ and T₂ preparation, resulting in a delay of about 20 ms between 92 segments to allow the gradients to be ramped down and up quietly. However, with a high number spokes per segment, 93 here 512, the duration of the segment is approximately 2.25 s and the delay between segments is only 20 ms, therefore μ the delay does not alter the steady state substantially. Cartesian images were collected with α=3.5° & 20°, TR=10.6 ms, TE=3.4 ms, parallel imaging factor=1.5 (ASSET), RF spoiling increment=115.4◦ ⁹⁵ . Total acquisition time of the RUFIS and ⁹⁶ SPGR protocols was matched to ≈2 mins per flip angle, 4 mins total, in both cases. γ Two sets of B₁⁺ maps were acquired; Bloch-Siegert [17] for correcting the SPGR data, and SIMBA for RUFIS data. ⁹⁸ Bloch-Siegert data were acquired using a 2D multi-slice sequence with an 8 ms Fermi pulse applied 4 kHz off resonance, \cdot readout parmeters: FA=15°, TE/TR=13.1/18 ms, in-plane resolution=4x4 mm², FOV=256x256 mm², 40 slices with ¹⁰⁰ 4 mm slice thickness, duration=1:40 min. SIMBA data were acquired using the 3D RUFIS sequence with readout $_{101}$ bandwidth= \pm 9.25 kHz, α=1 $^{\circ}$, 6x6x6 mm 3 resolution, 192x192x192 mm 3 FOV, 256 spokes per segment, preparation 102 α_{SAT} =5°, number of pulses in preparation train=[54,36,18,0], 3 s recovery time. Acquisition parameters were adjusted

 103 to achieve a total acquisition time of 1 minute. Each scanning session also included a sagittal T₁-weighted IR-SPGR $_{104}$ (BRAVO) for tissue segmentation with TE/TR/TI=3/7/400 ms, FOV=270x270x240 mm 3 , slice thickness=1.2 mm, in- $_{105}$ plane resolution=1.05x1.05 mm², FA=11°, BW=31.25 kHz, and ASSET=1.75.

¹⁰⁶ Four healthy volunteers were scanned twice with the same protocol, with an average time between scan sessions of 107 50 days (range: 48-52 days). In each session, the anatomical BRAVO image was acquired once and the VFA T₁-mapping

 $_{\rm 108}$ protocols using RUFIS and SPGR, with $\rm B_1^+$ correction, were acquired twice (without repositioning). All scans were ¹⁰⁹ collected under ethical approval by the Camberwell St Giles NHS (National Health Service) HRA (Health Research ¹¹⁰ Authority) Research Ethics Committee and participants gave written informed consent.

 $_{111}$ The protocol details above were also used to scan a quantitative phantom consisting of 12 vials with a range of T_1 112 values (T₁=200-1500 ms, EUROSPIN test object 5 (TO5)[18]). Vials were mounted in an in-house made styrofoam mount. $\rm _{113}$ $\rm \,$ Due to the small size of the vials (≈2 cm in diameter), an additional SIMBA scan with higher resolution (4x4x4mm 3) was 114 acquired for the phantom experiment. Increasing the resolution also increased the TR to 1.6 ms which was accounted 115 for by reducing the number of spokes per segment to 176, to maintain the same T_1 recovery during the readout.

¹¹⁶ Acoustic noise measurements were performed using a Casella (IDEAL Industries, Ill) CEL-63X sound meter with an 117 external microphone placed in the centre of the bore, mounted to a cylindrical water phantom with padding between 118 the phantom and microphone to avoid vibrations. Measurements were taken throughout each of the scans with a $_{119}$ sampling rate of 1 sample every 2 s. Within a 40 s segment for each sequence, the average A-weighted equivalent sound 120 level (LAEQ [dBA]) and C-weighted peak sound level (LCPEAK [dBC]) were calculated.

¹²¹ **2.4** | **Image Reconstruction and Processing**

¹²² Data acquired with RUFIS were reconstructed offline in MATLAB (MathWorks, Natick, MA, USA). Radial k-space ¹²³ data were gridded using the Kaiser-Bessel method. Coil sensitivity maps were estimated using ESPIRiT, implemented 124 in the Berkeley Advanced Reconstruction Toolbox (BART) [19, 20, 21]. Images were reconstructed using a SENSE 125 reconstruction with 3D Total Variation regularization with $\lambda = 0.001$ implemented in the pics command in BART. For
126 SIMBA data, coil sensitivity mans were estimated from the centre of k-space using the method des SIMBA data, coil sensitivity maps were estimated from the centre of k-space using the method described by McKenzie 127 et al., also implemented in BART [22].

 $_{128}$ To calculate the SIMBA B₁⁺ map, real valued data is needed. Due to the effective TE=0 with RUFIS, no phase evolution is expected from the readout itself. The phase of the first image, with no preparation, was therefore subtracted from subsequent images, allowing positive signals to be distinguished from negative signals. The B⁺ map was then calculated through a non-linear fit of the real data to the following equation

$$
M = A \cdot \cos(\lambda \cdot n \cdot \alpha_{SAT}) + C. \tag{8}
$$

 To correct for the excitation profile in the RUFIS acquisition, an iterative simulation was performed where the excitation profile for individual spokes was calculated analytically using equation (3). The 3D excitation profile was calculated for spokes and then averaged. The simulated excitation profile was then multiplied by the SIMBA B $_1^+$ map to obtain a 135 total B_1^+ correction.

136 Data acquired with RUFIS and SPGR were motion corrected using mcFLIRT[23]. B $_1^+$ maps from SIMBA and Bloch-137 Siegert were registered and transformed to the space of the associated VFA acquisition using an affine transforma- $_{138}$ tion [24]. The transformed B⁺ maps were smoothed using a Gaussian kernel with 8 mm FWHM to reduce propagation 139 of noise into the T₁ maps. Quantitative T₁ and proton density maps were calculated using a linear fit, implemented in ¹⁴⁰ the QUantitative Imaging Tools (QUIT) [25]. The first RUFIS and SPGR acquisition within each scanning session were ¹⁴¹ registered to the BRAVO scan using a combined affine and non-linear registration[26, 24]. A non-linear transformation ¹⁴² was chosen as we observed minor differences in gradient distortions between the acquisitions, due to the different ¹⁴³ reconstruction pipelines used. The second VFA acquisition of each scanning session was registered to the first VFA ¹⁴⁴ acquisition using an affine transformation. This transformation was then combined with the non-linear transformation 145 to the BRAVO image.

 To obtain unbiased regions of interest (ROI) for analysis of the T_1 -maps, the BRAVO data for each subject and each visit were segmented using Freesurfer [27]. The following ROIs from the FreeSurfer analysis were used in the analysis: Pallidum (ID: 13+52), Thalamus (ID: 10+49), Caudate (ID: 11+50), Putamen (ID: 12+51), Corpus Callosum (CC) posterior (ID: 255), CC anterior (ID: 251), cerebral white matter (WM) (ID: 2+41), cerebral cortex (ID: 3+42). FreeSurfer ROIs were warped to the native space of the VFA data using the previously calculated transformations in a single step with MultiLabel interpolation [24]. Average T₁ values were calculated within each ROI, bilateral ROIs were averaged.

The image analysis pipelines were developed using the nipype framework [28].

2.5 | **Statistical Analysis**

 Repeated scans within the same session were treated as measurements performed under identical conditions, defined as repeatability conditions [29], and analysed using the methods described by Bland and Altman[30]. Within each visit, ¹⁵⁶ each sequence, and each ROI, the mean (\bar{d}) and standard deviation (s_d) of the difference between repeated scans across 157 the subjects were calculated. The coefficient of repeatability (CoR) was calculated as $CoR_w = 2s_d$, with subscript w indicating within visit. The CoR is an aggregate measure of the absolute variability in the data, i.e. it does not scale with the true T₁ within the ROI. Another value often reported in the literature is the coefficient of variation (CoV), this is ¹⁶⁰ calculated per subject as $CoV_w = 100 \cdot std(y_1, y_2)/mean(y_1, y_2)$ where y_1 and y_2 are the test-retest T₁ values within the covis defined the SOL Since the CoV is defined same session. The CoV is a percentage estimate, which is scaled by the true T₁ inside the ROI. Since the CoV is defined in terms of a standard deviation, its statistical validity is limited when only a small number of measures are used to calculate it, and its value could be questioned in a study such as the current one with only two measurement points, results from CoV analysis are therefore only provided in the supporting information for comparison to the literature. 165 Low CoR and CoV indicates high repeatability.

 Repeated scans at the two different time points (i.e. visits), were treated as measurements taken under reproducibil- ity conditions[29], with day-to-day biological variation and conditions in the scan room being factors not held constant. ¹⁶⁸ All other parameters were matched between the two scans. The within subject test-retest mean and difference in T_1 were utilized for the reproducibility analysis. The average difference between the test-retest values at each time point (D) and the standard deviation (s_D) across subjects were calculated. The corrected standard deviation of the mean of the differences was calculated as $s_c = \sqrt{s_D^2 + \frac{1}{4}s_{d,1}^2 + \frac{1}{4}s_{d,2}^2}$ [30], where $s_{d,1}$ and $s_{d,2}$ are the standard deviation of the the differences was calculated as $3e^2 = \sqrt{9b} + \frac{49d}{3} + \frac{1}{4} + \frac{49d}{3}$ where $3a$ ^r and $3a$ _{r2} are the standard deviation of the test-retest differences at the two time points. The coefficient of reproducibility w 173 coefficient of variability as $Cov_b = 100 \cdot std(y_1, y_2)/mean(y_1, y_2)$ where y_1 and y_2 are the average T₁ values for visit 1
174 and 2 for each subiect. Subscript *b* here indicates between visits. and 2 for each subject. Subscript b here indicates between visits.

 Comparison of T₁ between the two sequences was performed using both in vivo and phantom data. With the in vivo data, whole brain histograms were calculated, and Bland-Altman plots of the isolated ROIs from all subjects were produced. Using the phantom data, Bland-Altman analysis was used to compare T_1 values within the individual vials.

3 | **RESULTS**

3.1 \parallel **B**⁺-mapping with SIMBA

The calculated $\mathsf B_1^+$ map from SIMBA is shown in figure 3 along with the Bloch-Siegert $\mathsf B_1^+$ map for comparison. The $\mathsf B_1^+$ $_{\rm 181}$ maps have been transformed to VFA space and smoothed as previously described. The B $_1^+$ field estimated by SIMBA was lower than Bloch-Siegert, a pattern that was also observed in the other subjects and in the repeated scans. Without any correction the RUFIS R₁ maps showed strong inhomogeneity around the edges of the brain, see 3 C. Applying B $_1^+$

- 184 correction to the RUFIS data with SIMBA and Bloch-Siegert showed similar improvements to the homogeneity in the R₁.
- 185 However a shift in T₁ towards shorter values was observed when Bloch-Siegert was used for correcting RUFIS data,
- ¹⁸⁶ compared to using SIMBA, as shown in figure 3 D.

<code>FIGURE 3</code> $\,$ Comparison of B_1^+ maps acquired with SIMBA (A) and Bloch-Siegert shift (B). SIMBA produces slightly lower B_1^+ values, as seen by the contour lines. R_1 (1/ \mathcal{T}_1) maps calculated from RUFIS VFA data without B_1^+ correction show strong inhomogeneity (C). Applying SIMBA or Bloch-Siegert B_1^+ correction shows clear improvement. (D) Comparing T $_1$ maps from RUFIS with Bloch-Siegert and SIMBA B_1^+ -correction shows a consistent shift towards lower T_1 values, with no obvious spatial variation, when Bloch-Siegert is used. (The R₁ map is shown instead of T₁ as it better highlights the effects of the B_1^+ correction.)

¹⁸⁷ **3.2** | T1**-mapping**

 $_{^{188}}$ $\,$ An overview of the T $_1$ and PD maps from the first visit from RUFIS, with SIMBA $\mathsf B_1^+$ correction, and SPGR, with Bloch- $_{189}$ Sieger B $^+_1$ correction, is presented in figure 4. Qualitatively, the T $_1$ maps from RUFIS looked very similar to SPGR in ¹⁹⁰ the brain and the histograms, shown in 5, also overlap to a great extent. One noticable difference between the two 191 acquisitions is outside the brain. The ZTE readout in RUFIS captures the short T_2 signal from the skull which can be seen 192 clearly in the proton density and T₁ maps. The location of the WM peak in the T₁ histograms is similar between RUFIS 193 and SPGR, with an average difference for the WM peak of ∆*W M_{peak}* = 70 ± 40 ms. However, a greater variability was 194 observed for GM, $\Delta GM_{peak} = -180 \pm 70$ ms. This is also reflected in the Bland-Altman plot comparing T₁ values from ¹⁹⁵ RUFIS and SPGR within isolated ROIs presented in figure 6A, which shows larger difference for GM structures. Average 196 T₁ values between the two repeated scans in the first visit, within isolated ROIs, are shown in table 1.

 197 Similar results were observed in the phantom experiments. The RUFIS and SPGR T₁ values were found to be 198 highly correlated (Pearson's $\rho = 0.93$), but Bland-Altman analysis (figure 6B) showed a trend for larger differences in T₁
199 between the two sequences for longer T1, with an average difference in T1 across all vi between the two sequences for longer T₁, with an average difference in T₁ across all vials of $\bar{d} = -0.4$ s, and standard
₂₀₀ deviation of the mean of *s_d* = 0.4 s. deviation of the mean of $s_d = 0.4$ s.

²⁰¹ The average within session repeatability for all ROIs for the two visits were comparable between the two sequence;

FIGURE 4 Example of quantitative T_1 and proton density maps from one subject acquired with RUFIS and Cartesian SPGR. Due to the ZTE readout in RUFIS, a T_1 fit could be obtained in the cortical bone, indicated by the white arrows, and a higher proton density was observed in the same area.

FIGURE 5 T_1 -histograms of whole brain white matter and cortical gray matter from all four subjects from the first visit, averaged over the two scans.

202 RUFIS $\text{C} \sigma R_{w,1}/\text{C} \sigma R_{w,2} = 0.06/0.02$, SPGR $\text{C} \sigma R_{w,1}/\text{C} \sigma R_{w,2} = 0.05/0.08$. Better between sessions average reproducibil-
202 ity between all ROIs was found for RUFIS ($\text{C} \sigma R_{w} = 0.07$) compared to ²⁰³ ity between all ROIs was found for RUFIS (CoR_b = 0.07) compared to SPGR (CoR_b = 0.2). Table 1 summarises the
²⁰⁴ repeatability and reproducibility estimates from each individual ROI. The CoV values can be foun repeatability and reproducibility estimates from each individual ROI. The CoV values can be found in table S1 in the ²⁰⁵ supporting information.

²⁰⁶ **3.3** | **Acoustic Noise Measurements**

₂₀₇ Table 2 shows average LAeq and LCpeak values from the acquisitions used in the protocol along with the ambient noise level in the scan room. RUFIS showed no measurable increase in sound pressure levels, but the sequence is in practice still just audible as it produces a higher pitched sound than the background noise (e.g. compressor pump) in the scan room. These measurement are comparable to those reported by Alibek et al., who measured a non-significant increase of 0.07 dB between RUFIS and ambient noise levels [31]. Costagli et al. measured an increase of 2.5dBA for RUFIS $_{212}$ compared to ambient noise levels, however, the ambient noise level in their scan room was 52.7 dBA which is much

F I G U R E 6 Bland Altman analysis comparing RUFIS and SPGR in vivo **(A)**, and in the EUROSPIN quantitative phantom (B). Both in vivo and phantom experiment showed lower T₁ estimates from RUFIS for longer T₁. Data is from first scan at first visit for both in vivo and phantom data.

213 lower than what we measured [9]. The increased acoustic noise during the SIMBA acquisition is due to the spoiling $_{214}$ gradients after the preparation module.

²¹⁵ **4** | **D ISCUSS ION**

²¹⁶ **4.1** | **Silent T**1**-mapping**

 $_{217}$ The acoustic noise produced by the MRI scanner during data acquisition is commonly reported by patients as one of 218 the main unpleasant features of the scanning experience [32, 33]. In this work we have shown that the silent RUFIS $_{219}$ sequence can be used for T₁-mapping together with a novel, silent, B⁺ mapping method, SIMBA. We compared RUFIS to $_{220}$ Cartesian SPGR and found that the two sequences produced comparable T₁ maps. The agreement between the two $_{221}$ sequences was best in white matter, while in gray matter a longer T_1 was observed with SPGR. These results were also ₂₂₂ reflected in our phantom experiment. We found comparable in vivo repeatability between the two sequences, but ²²³ reproducibility was better for RUFIS.

224 With no previous studies using RUFIS for VFA T_1 mapping, we can only compare our results to literature using non- 225 ZTE acquisitions. Quantitatively, our T₁-values compares well with previous literature such as Stanisz et al. reporting $_{226}$ T₁=1084 \pm 45/1820 \pm 114 in WM/GM[34]. In terms of reproducibility, our results also align with previous studies. Deoni 227 et al. reported whole brain, voxel wise, intra-site CoV from SPGR VFA T₁-mapping of 6.4 [35]. Similar results were 228 presented by Weiskopf et al. using VFA, reporting R_1 intra-site CoV of 3.9 and 4.7 in the corpus callosum and caudate 229 nucleus repspectively[36]. However, the small sample size (N=4) and only two visits limit the conclusions that can be ²³⁰ drawn from the current study.

²³¹ There are several differences in the data acquisition between the two sequences that could contribute to the $_{232}$ observed difference in T₁. The signal equation used assumes full spoiling of the transverse magnetisation. For SPGR, ²³³ spoiling was achieved by RF and separate gradient spoiling after the readout. In RUFIS, spoiling was mainly achieved ²³⁴ using RF spoiling, together with some gradient spoiling from the readout gradients. Previous work by Deichmann et al. 235 showed that corrections for insufficient spoiling can be applied to improve T_1 reproducibility across different scan 236 protocols [37], and it is therefore possible that some of the variability in T_1 between RUFIS can be attributed to the ₂₃₇ different spoiling behaviour. However, the algorithm used by Deichmann et al. assumed gradient spoiling along one axis ²³⁸ after the readout, which does not apply for RUFIS. Furthermore, previous studies of spoiling behaviour in radial gradient

TABLE 1 T_1 values in isolated ROIs averaged between the two scans in the first visit together with within session repeatability estimates (CoR_w) from the first visit and between sessions reproducibility measurements (CoR_b). Lower values of CoR are better

TABLE 2 Summary of acoustic noise measurements from each sequence. Values are reported as mean $\pm \sigma$ noise levels over a 40 s period. The large standard deviation in the noise levels for SIMBA is due to the periodic spoiling gradients. (LAEQ - A-weighted equivalent continuous sound level, LCPEAK - C-weighted peak sound level)

²³⁹ echo sequences suggests that random RF spoiling increment and gradient moments can produce ideal spoiling [38, 39]. ²⁴⁰ Corrections for insufficient spoiling in RUFIS will require modelling of spoiling along all three axes, which will be the

 $_{241}$ focus of future work.

242 Another difference between the two sequences is the RF pulses for excitation: RUFIS used hard pulses, while ²⁴³ SPGR used shaped pulses used for slab-selective excitation. Differences in pulse shape, and flip angles, between RUFIS 244 and SPGR could contribute to magnetisation transfer effects, which have been shown to affect T_1 measurements [40]. ²⁴⁵ The excitation profile in RUFIS was corrected for using a first order correction. However, as the readout direction ²⁴⁶ changes for each spoke, the effective flip angle at any point in space, except isocentre, will change over time. A first 247 order correction will make the effective flip angle equal to the average flip angle over time, and thus spin history effects $_{\rm 248}$ are neglected. The lower average B $_1^+$ efficiency and stronger effect of the excitation profile around the edges of the brain 249 could contribute to the difference in T₁ in cortical GM between the two sequence. However, we also see a difference in $_{250}$ T₁ in deep GM structures, suggesting a non-spatial phenomenon.

 $_{251}$ Methods for reducing the acoustic noise in MRI scanning, can broadly be categorised as; hardware modifications 252 [41, 42] or pulse sequence modifications, mainly through soft gradient pulses [43, 44, 45, 46]. In contrast, the silent properties of RUFIS arise naturally from the gradient ordering of the sequence, and so performance is not compromised. Previous studies have used RUFIS for silent imaging including T₂-prepared fMRI [47], and structural imaging at 3T [31] $_{255}$ and 7T [9]. Another silent ZTE sequence is Looping Star which uses gradient echoes for T $_2^*$ weighted imaging [48]. Our acoustic noise measurement showed no measurable increase in the sound pressure levels during RUFIS scanning compared to background noise levels, similar to Alibek et al. [31]. However, the quoted decibel values will differ depending on the scan room environment and are not necessarily what the subject would experience inside the scanner. ₂₅₉ The acoustic noise will also change depending on scan parameters such as the TR and number of spokes. Nevertheless, 260 we do not envisage any greater acoustic disturbance than measured herein.

²⁶¹ We chose to use a relatively low readout bandwidth (7.8 kHz) for the RUFIS acquisition in this study as our ²⁶² sequence optimisation showed that this would enable the most optimal VFA flip angle sampling scheme. However, lower ²⁶³ bandwidth will widen the point spread function and increase chemical shift artefacts [49]. In a 3D radial acquisition, chemical shift artefacts manifest in three dimensions as a spherical artefact. The chemical shift does not appear to ²⁶⁵ be a major issue in our study at 3T, but translating this technique to higher field strength will require higher readout bandwidth.

4.2 | **Silent B**⁺ ²⁶⁷ ¹ **mapping**

 $_{268}$ T₁ mapping using VFA is inherently sensitive to errors in the B⁺ map estimation. As shown by equation (2), and previously 269 by other authors, the apparent T_1 scales with the square of the flip angle bias field [13, 14]. In this study, we chose to $_{270}$ compare two complete protocols for T₁ mapping including B⁺ mapping. We chose to use the Bloch-Siegert method for $_{271}$ $\,$ $\rm B_1^+$ correction of the Cartesian SPGR data, as it is a standard sequence on the GE platform. This is not a silent sequence, 272 however, and therefore we developed a new method for silent B_1^+ mapping (SIMBA), specifically designed for correction ²⁷³ of RUFIS data. A train of hard RF pulses was used for magnetisation saturation to match the RUFIS acquisition as closely 274 as possible. SIMBA could also be used with a single saturation pulse with different flip angles to match the excitation 275 pulse in other sequences as well.

 $_{\rm 276}$ Comparison of the two B $_1^+$ mapping techniques revealed overall lower B $_1^+$ with SIMBA than Bloch-Siegert. Process- $_{\rm zzz}$ ing RUFIS VFA data with both B $_1^+$ techniques, figure 3, showed that the difference between the two techniques results $_{278}$ in a global uniform scaling of the T₁ values towards lower T₁ with Bloch-Siegert. Our comparison of T₁ values between 279 SPGR and RUFIS showed longer T₁ in GM with Bloch-Siegert corrected SPGR data compared to SIMBA corrected ²⁸⁰ RUFIS. Using Bloch-Siegert with RUFIS would therefore increase the difference between the sequences. It is therefore 281 unlikely that the observed differences in T₁ between the two sequences is caused by the B⁺ map.

²⁸² **4.3** | **Zero TE effects**

283 One aspect of the RUFIS sequence that has not been studied in this work is the zero echo time (ZTE) readout, which 284 results in sensitivity to short T₂ components, otherwise invisible to MR acquisitions [11, 12]. The ZTE effects can be 285 observed in the T₁ and PD maps obtained with RUFIS, where a much higher proton density and better T₁ fit was observed 286 in the cortical bone which has a very short T_1 and T_2 , see white arrows in figure 4. Recent works have suggested that ²⁸⁷ the ultra short T₂ component from the myelin lipids are visible using ZTE and ultra short TE (UTE) acquisitions [50, 51]. ²⁸⁸ However, the low bandwidth used in this work means that the signal from the solid myelin components will decay within ₂₈₉ the first few samples, and would, if anything, only contribute to an increased point spread function. Therefore, it is 290 unlikely that the ZTE properties of RUFIS contribute to the observed differences in T_1 between RUFIS and SPGR.

5 | **CONCLUS IONS**

 T₁ mapping with the VFA method using spoiled gradient echo imaging (SPGR) is a highly efficient method for T₁ mapping $_{293}$ but requires an additional B_1^+ map for correction of the B_1^+ field. RUFIS is a zero TE, silent imaging sequence with a spoiled free induction decay (FID) readout which effectively can be used for quantitative imaging using the same signal equations as SPGR. In this work we have shown that RUFIS can be used for silent VFA T₁ mapping with results that are $_{296}$ very similar to a conventional Cartesian SPGR acquisition. A novel silent B₁⁺ mapping technique based on RUFIS was $_{\rm 297}$ also presented which can provide the necessary $\mathsf B_1^+$ correction for VFA T $_1$ mapping using RUFIS.

 $_{298}$ We demonstrated a fully silent VFA T₁ and B⁺₁ mapping protocol with higher reproducibility and comparable repeatability compared to the equivalent standard Cartesian SPGR sequence. Adoption of this protocol could lead to increased patient comfort in quantitative imaging studies.

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309 directly.

310 **APPENDIX**

³¹¹ **5.1** | **Derivation of the quantitative RUFIS signal equation**

 312 We begin from the results derived by Hsu and Lowe[52]. Let the longitudinal magnetisation of spoke n in segment m be 313 $M_z(n, m)$. With N spokes per segment we get

$$
M_Z(n,m) = M_Z(0,m) \cdot \cos^n(\alpha) E_1^n + \rho(1 - E_1) \cdot \frac{1 - \cos^n(\alpha) E_1^n}{1 - \cos(\alpha) E_1}
$$
 (9)

³¹⁴ where $E_1 = e^{-TR/T_1}$, α is the excitation flip angle, and ρ is the proton density. If $n \to \infty$ then cosⁿ(α) → 0, and (9) 315 approaches the well known gradient echo steady state signal equation

$$
\lim_{n \to \infty} M_z(n, m) = \rho \cdot \frac{1 - E_1}{1 - \cos(\alpha) E_1} = M_{z, spgr}
$$
\n(10)

316 To simplify (9), we set $\xi = \cos(\alpha)E_1$ and substitute in $M_{z,spgr}$ to obtain

$$
M_z(n,m) = M_z(0,m) \cdot \xi^n + M_{z,spgr} \cdot (1 - \xi^n). \tag{11}
$$

 317 With a segment of N spokes, the acquired magnetisation is proportional the average available longitudinal magnetisation 318 of all spokes. This can be formulated as

$$
\bar{M}_z(m) = \frac{1}{N} \sum_{i=0}^{N-1} M_z(i, m) = \frac{1}{N} \sum_{i=0}^{N-1} \left(M_z(0, m) \cdot \xi^i + M_{z, spgr} \cdot (1 - \xi^i) \right) = M_z(0, m) \cdot f + M_{z, spgr}(1 - f) \tag{12}
$$

319 where

$$
f = \frac{1}{N} \sum_{i=0}^{N-1} \xi^{i} = \frac{1}{N} \frac{1 - \xi^{N}}{1 - \xi} = \frac{1}{N} \frac{1 - (\cos \alpha \cdot e^{-TR/T_{1}})^{N}}{1 - \cos \alpha \cdot e^{-TR/T_{1}}}. \tag{13}
$$

 320 Index runs from 0 to N – 1 as the acquired magnetisation is proportional to available magnetisation before each spoke.

 321 When data is collected in a steady state, the inter-segment delay (τ) will cause intermittent T₁ recovery. The 322 effect of this will depend on the number of spokes per segment as well as τ . The effect of this delay can be calculated 323 analytically. The magnetisation at the beginning of segment $m + 1$ is proportional to the magnetisation at the end of the 324 previous segment as well as the T₁ recovery between segments as

$$
M_Z(0, m+1) = M_Z(N, m) \cdot e^{-\tau/T_1} + \rho (1 - e^{-\tau/T_1}).
$$
\n(14)

325 Combining (14) with (11) yields

$$
M_Z(0, m+1) = \left[M_Z(0, m) \cdot \xi^N + M_{Z, spgr} \cdot (1 - \xi^N) \right] e^{-\tau/T_1} + \rho (1 - e^{-\tau/T_1}). \tag{15}
$$

If the magnetisation at the beginning of each segment has reached a steady state (\tilde{M}_0) we can substitute $M_z(0,m+1)$

and $M_z(0, m)$ with \tilde{M}_0 in (15) and solving for \tilde{M}_0 to get

$$
\tilde{M}_0 = M_{z, spgr} \cdot \frac{e^{-\tau/T_1}(1 - \xi^N)}{1 - \xi^N e^{-\tau/T_1}} + \rho \frac{1 - e^{-\tau/T_1}}{1 - \xi^N e^{-\tau/T_1}}.
$$
\n(16)

SUPPORTING INFORMATION

 Table S1 Within the first visit and between sessions coefficient of variation (Cov_w / Cov_b) for RUFIS and SPGR T₁ measurements. Lower values indicate higher repeatability and reproducibility. Values reported as mean± σ .

R E F E R E N C E S

- 330 [1] Christensen KA, Grant DM, Schulman EM, Walling C. Optimal determination of relaxation times of fourier transform nuclear magnetic resonance. Determination of spin-lattice relaxation times in chemically polarized species. The Journal of Physical Chemistry 1974;78(19):1971–1977. http://pubs.acs.org/doi/abs/10.1021/j100612a022.
- 333 [2] Gupta RK. A new look at the method of variable nutation angle for the measurement of spin-lattice relaxation times using fourier transform NMR. Journal of Magnetic Resonance 1977;25(1):231–235.
- [3] Homer J, Beevers MS. Driven-equilibrium single-pulse observation of T1 relaxation. A reevaluation of a rapid "new" method for determining NMR spin-lattice relaxation times. Journal of Magnetic Resonance (1969) 1985;63(2):287– 297.
- [4] Fram EK, Herfkens RJ, Johnson GA, Glover GH, Karis JP, Shimakawa A, et al. Rapid calculation of T1 using variable flip angle gradient refocused imaging. Magnetic Resonance Imaging 1987;5(3):201–208.
- 340 [5] Deoni SCL. High-Resolution T1 Mapping of the Brain at 3T with Driven Equilibrium Single Pulse Observation of T1 with High-Speed Incorporation of RF Field Inhomogeneities (DESPOT1-HIFI). Journal of Magnetic Resonance Imaging 2007;26:1106–1111.
- [6] Wang HZ, Riederer SJ, Lee JN. Optimizing the precision in T1 relaxation estimation using limited flip angles. Magnetic Resonance in Medicine 1987;5(5):399–416.
- 345 [7] Deoni SCL, Rutt BK, Peters TM. Rapid combined T1 and T2 mapping using gradient recalled acquisition in the steady state. Magnetic Resonance in Medicine 2003;49(3):515–526.
- [8] Madio DP, Lowe IJ. Ultra-Fast Imaging Using Low Flip Angles and FIDs. Magnetic resonance in medicine 1995;34(4):525– 529.
- [9] Costagli M, Symms MR, Angeli L, Kelley DAC, Biagi L, Farnetani A, et al. Assessment of Silent T1-weighted head imaging at 7 T. European Radiology 2016;26(6):1879–1888. http://dx.doi.org/10.1007/s00330-015-3954-2.
- [10] Weiger M, Pruessmann KP. MRI with Zero Echo Time. eMagRes 2012;1:311–322.
- 352 [11] Wiesinger F, Sacolick LI, Menini A, Kaushik SS, Ahn S, Veit-Haibach P, et al. Zero TE MR bone imaging in the head. Mag-netic Resonance in Medicine 2016;75(1):107–114.
- [12] Gibiino F, Sacolick L, Menini A, Landini L, Wiesinger F. Free-breathing, zero-TE MR lung imaging. Magnetic Resonance Materials in Physics, Biology and Medicine 2015;28:207–215. http://dx.doi.org/10.1007/s10334-014-0459-y.

356 [13] Helms G, Dathe H, Dechent P. Quantitative FLASH MRI at 3T using a rational approximation of the Ernst equation. Magnetic Resonance in Medicine 2008;59(3):667–672.

- [51] Boucneau T, Cao P, Tang S, Han M, Xu D, Henry RG, et al. In vivo characterization of brain ultrashort-T2 components. Magnetic Resonance in Medicine 2017;00(November):1–10. http://doi.wiley.com/10.1002/mrm.27037.
- 437 [52] Hsu JJ, Lowe IJ. Spin-lattice relaxation and a fast T1-map acquisition method in MRI with transient-state magnetization. Journal of Magnetic Resonance 2004;169(2):270–278.

SUPPORTING INFORMATION

TABLE S1 Within the first visit and between sessions coefficient of variation (Cov_w / Cov_b) for RUFIS and SPGR T₁ measurements. Lower values indicate higher repeatability and reproducibility. Values reported as mean±σ.