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9 **CONTROL OF SHROUD LEAKAGE LOSS AND WINDAGE TORQUE IN A LOW-PRESSURE**  
10 **TURBINE STAGE**  
11

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12  
13 **ABSTRACT**

14 *As new aeroengine architectures move to larger diameter*  
15 *fans and rotors, the associated increase in weight will need to be*  
16 *counterbalanced by lighter, more compact, and more efficient*  
17 *low-pressure turbines (LPT). Efficiency gains in LPTs can be*  
18 *achieved by reducing the losses associated with the shroud*  
19 *leakage flows. Flow control studies on the topic have*  
20 *traditionally focused on reducing the mixing loss, which*  
21 *constitutes a considerable proportion of the total loss.*  
22 *Nonetheless, increasing engine speeds are driving additional*  
23 *gains obtained by also targeting the reduction of windage losses.*  
24 *Developing a flow control solution with the dual objective of*  
25 *reducing over-tip cavity mixing and windage losses has not*  
26 *previously been attempted. This is a challenge due to conflicting*  
27 *flow control requirements and geometric constraints. Reducing*  
28 *windage loss generally requires increasing the swirl-ratio of the*  
29 *leakage flow, while reducing mixing loss requires reducing this*  
30 *ratio to match that of the main gas path. The current work*  
31 *proposes a novel flow control solution to successfully achieve*  
32 *this purpose through the emerging technology of additive*  
33 *manufacturing. The successful flow control concept was*  
34 *developed through numerical simulation, printed using an*  
35 *additive manufacturing process, and validated in a purpose-built*  
36 *rig. Experiments and computations were consistent with a*  
37 *cumulative reduction in cavity windage of 16%. The FCC*  
38 *is estimated to increase the mechanical efficiency of the turbine*  
39 *stage in isolation by 1%.*

40 **Keywords:** Turbines, Cavities, Sealing, Windage, Mixing,  
41 Flow Control, CFD.

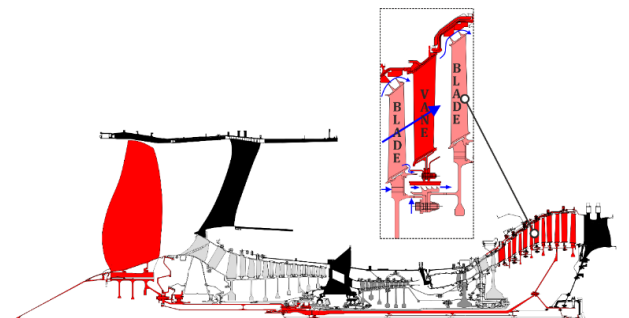
42  
43 **1. INTRODUCTION**

44 Minimizing the losses within a low-pressure turbine (LPT)  
45 system is critical for the design of next-generation ultra-high  
46 bypass ratio aero-engines. These new engines will host larger

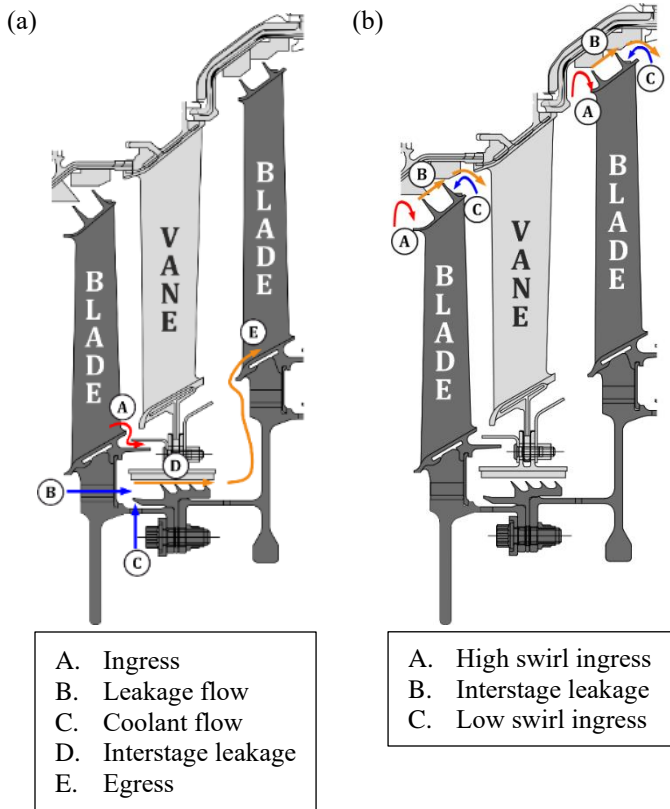
47 diameter fans and operate at higher rotor speeds. It is expected  
48 that windage torque in the stator-well and over-tip cavities will  
49 be a significant source of loss, influenced by the ingestion of  
50 mainstream annulus air with a tangential velocity opposite to that  
51 of the rotor.

52 A low-pressure turbine features a series of cavities at high  
53 and low radius, which aim to prevent ingestion and leakage of  
54 mainstream annulus air. Figure 1 highlights the cross-section of  
55 the LPT in a three-spool aero-engine. The inset shows 1.5 stages  
56 of the LPT in more detail (rotor-stator-rotor). At low radius, a  
57 stator-well cavity is formed of two wheel-spaces, connected by  
58 an interstage labyrinth seal. At high radius, the rotor shroud and  
59 fin tips form an over-tip cavity with the casing.

60 A stator-well cavity is shown in detail in Fig.2a. This  
61 configuration has been a recent subject of research through the  
62 EU Clean Sky 2 Programme [1-3]. The salient flow paths include  
63 ingress into the upstream wheel-space of the cavity (A), leakage  
64 through small tangential blade gaps (B), cooling flow (C),  
65 interstage leakage (D) minimized by the labyrinth seal on the  
66 axial drive arm of the rotor, and egress to the mainstream annulus



**FIGURE 1: CROSS-SECTION OF A MODERN THREE-SPOOL AERO-ENGINE WITH THE LOW-PRESSURE SYSTEM IN RED.**



**FIGURE 2:** FLOW PATHS IN (a) A STATOR-WELL CAVITY, AND (b) AN OVER-TIP CAVITY.

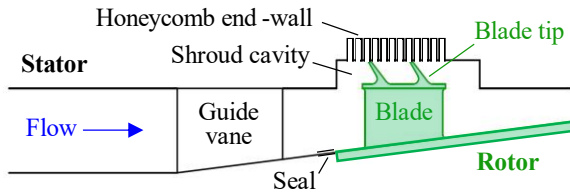
68  
69 (E). The flow paths in an over-tip cavity are shown in Fig.2b.  
70 Here the flow approaches the blade with a high swirl (positive).  
71 Some of this positively swirling flow is ingested into the  
72 upstream chamber of the over-tip cavity (labelled A). Since this  
73 has high, positive swirl, the relative windage contribution in the  
74 upstream chamber is small. A portion of this ingress will bypass  
75 the blade passage and instead traverse the fin tips (B), despite a  
76 small radial clearance achieved using an abradable lining (often  
77 honeycomb) on the casing. This interstage leakage will exit the  
78 downstream chamber as egress to the main annulus with a  
79 difference in swirl angle (the blade row has turned the flow from  
80 positive to negative swirl), causing an associated mixing loss.  
81 Some of the negative swirl will also be ingested into the  
82 downstream chamber (C), resulting in a windage loss due to the  
83 proximity of the negative swirl with the downstream rotor tip fin.

84 Experimental and numerical investigations of over-tip  
85 cavity flows reveal complex flow interactions between cavity  
86 and main flow, with the underlying mechanisms still a matter of  
87 debate [4-6]. Measurements from the exit cavity of a stationary  
88 blade row labyrinth system showed the existence of non-uniform  
89 flow with high circumferential velocity [4]. Highly-resolved  
90 flow data collected from the inlet cavity of a turbine rotor tip  
91 labyrinth seal revealed a toroidal vortex at the interface with the  
92 main flow [5]. Perini et al. [6] analyzed rotating instabilities  
93 formed inside an LPT over-tip cavity and identified unsteady  
94 flow structures uncorrelated with the blade-passing frequency.

95 The complex flow interactions uncovered in these studies  
96 generate the so-called mixing losses [7, 8] but can also dominate  
97 the secondary flow inducing further losses downstream; the  
98 extent of influence depend on the clearances in the cavity among  
99 other parameters [9, 10]. The influence of radial gap and exit  
100 cavity size on yaw angle in the near-tip region of the main flow  
101 were also assessed through numerical simulation in an over-tip  
102 cavity model in a two-stage LPT [11]. Mixing loss is the creation  
103 of entropy due to viscous friction between the differing velocity  
104 streams of the main gas path and the re-entering leakage flow.  
105 This thermodynamically irreversible process causes a decrease  
106 of the stagnation pressure and an increase of the turbulence  
107 kinetic energy. In the current work, the mixing loss was  
108 visualized as a change in turbulence kinetic energy but quantified  
109 more precisely with the calculation of an isentropic efficiency  
110 for the turbine stage in isolation.

111 In terms of flow control concepts, Phau et al. [12] proposed  
112 design modifications such as non-axisymmetric profiling on the  
113 shroud based on the flow understanding gained from their  
114 experimental analysis of over-tip cavity flow structure. These  
115 were not evaluated rigorously but were predicted to offer a  
116 potential 0.2%-0.5% improvement in overall turbine efficiency.  
117 Later work investigated the use of turning vanes on the stator and  
118 rotor. A turbine rig was used to introduce a vane row in the  
119 downstream region of an over-tip cavity, which was shown to be  
120 effective in reducing loss by turning the leakage in the direction  
121 of the mainstream annulus flow [13]. The LPT efficiency  
122 increased by up to 0.4%, with the performance dependent upon  
123 the vane geometry and their spacing. Additional profile features  
124 were investigated in a separate study using the same  
125 experimental facility [14]. Results showed that chamfering and  
126 profiling the end wall and adding axial and radial deflectors all  
127 improved the stage efficiency. An optimized solution with a  
128 combination of these features generated an overall efficiency  
129 improvement of 0.75%. Wallis et al. [15] found that turning  
130 vanes on the rotor shroud reduced the tip leakage flow. Despite  
131 the intention to extract additional work from the vanes, the  
132 efficiency reduced owing to increased ingress into the  
133 downstream cavity, because of the reduced leakage. However,  
134 computational results show that turning vanes on the casing can  
135 improve the turbine efficiency if they are successful at turning  
136 the flow in the direction of the mainstream [16]. Passive tip-  
137 injection is a further flow control strategy that has been explored  
138 numerically by Ghaffari et al. [17] for a realistic LPT stage,  
139 where boundary conditions were taken from experiment without  
140 tip-injection. The principle of this approach was to apply  
141 aerodynamic resistance to the leakage flow to reduce its mass  
142 flow rate. Although their results did not show any reduction in  
143 the overall leakage mass flow rate, it was argued that the injected  
144 flow that made up a portion of the leakage contributed to the  
145 specific work of the stage. Further, there was also enhancement  
146 of the yaw angle at the cavity outlet.

147 Although there is evidence of LPT cavity flow control to  
148 reduce mixing losses and the downstream stage losses, there is  
149 no substantive research on the application of methods to reduce  
150 cavity windage torque. Minimizing windage torque is critical for



**FIGURE 3: LOW-PRESSURE TURBINE STAGE**

the development of next-generation ultra-high bypass ratio aero-engines. This paper presents a joint numerical and experimental campaign on the application of an optimized flow control concept (FCC) to reduce both the windage torque and the mixing losses in an LPT over-tip cavity. The FCC was a row of turning deflectors in the downstream chamber of the over-tip cavity, which redirected positively swirling flow onto the back face of the rotor fin to reduce the windage, whilst also turning the over-tip leakage in the direction of the main annulus flow to minimize mixing losses. It was optimized to perform most effectively with the honeycomb end-wall at an operating point representative of cruise flight conditions. The paper is structured as follows: details of the numerical model and experimental facility are in section 2, validation of the baseline flow, i.e., the flow without the FCC, is in section 3, development of the FCC through numerical simulation is in section 4, validation of the FCC is in section 5, and conclusions are in section 6.

## 2. METHODOLOGY

The engine-representative geometry and boundary conditions for the LPT stage were provided by the Clean Sky 2 topic manager. These were used to prepare numerical and experimental models at the Universities of Nottingham and Bath, respectively. A schematic of the LPT stage is shown in Fig.3. It consists of 32 stator vanes (inlet guide vanes) and 33 rotor blades in a converging annulus. The over-tip cavity is formed by the fins (forward-angled teeth) on the rotor shroud and the casing. The outer casing is at a constant radius, with an interchangeable honeycomb or solid end-wall.

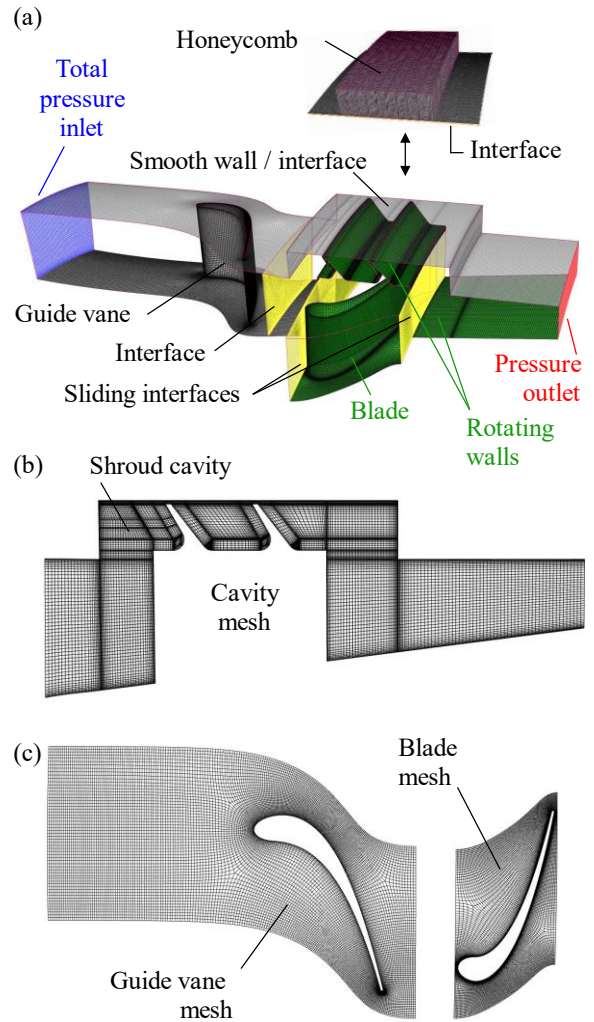
### 2.1 Numerical model

The numerical model was prepared using the commercial software ANSYS, version 2020R2, and is shown in Fig.4(a). The domain consisted of multiple cell zones that exchange flow data during the simulation through mesh interfaces. There were four cell zones: the guide vane, the cavity, the blade, and the honeycomb. The cavity was interfaced with the guide vane and honeycomb using static interfaces, and with the rotating blade using sliding mesh interfaces. The blade tip and the rotor hub surfaces in the static cavity cell zone were defined as rotating no-slip walls. The inlet upstream of the guide vane was defined as a total pressure inlet. The outlet downstream of the blade was defined as a static pressure boundary, with prescribed pressure at the inner radius and a radial pressure distribution given by Eq.1, where  $p$  is static pressure,  $r$  is the radial coordinate,  $\rho$  is density, and  $V_t$  is the tangential velocity component. This radial pressure distribution eliminated backflow at the outlet. All other surfaces,

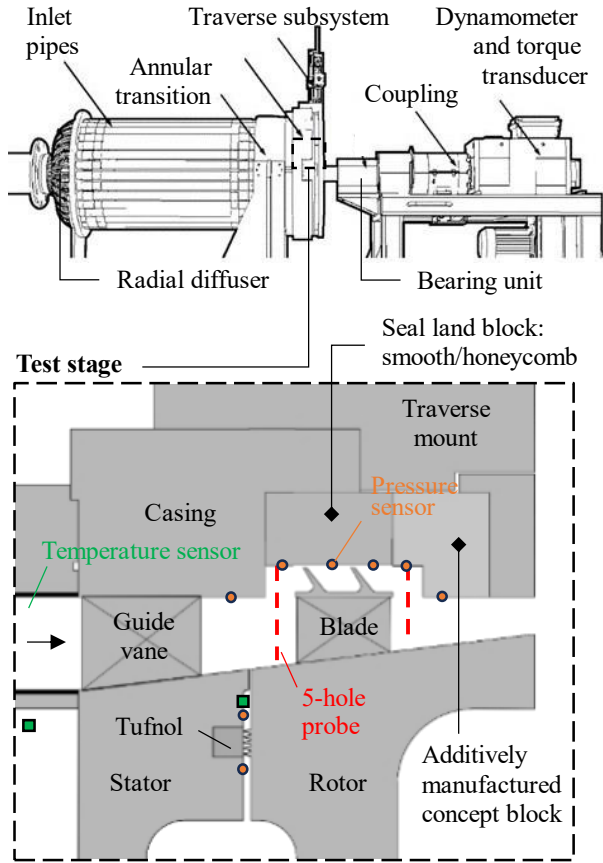
not explicitly referred to here, were defined as static no-slip walls. The angular velocity of the rotating cell zone and wall surface zones, the total pressure at the inlet, and the inner pressure at the outlet were matched to the rig operating conditions.

$$\frac{\partial p}{\partial r} = \frac{\rho V_t^2}{r} \quad (1)$$

Hexahedral meshes were generated for the cavity in ANSYS ICEM, and for the guide vane and blade blocks in ANSYS Turbogrid. The cavity mesh is shown in Fig.4(b). The guide-vane / blade meshes are shown in Fig.4(c); these and the rounded corners at the base of the teeth of the labyrinth seal teeth featured an o-grid topology. For the honeycomb, a tetrahedral mesh was generated in ANSYS Meshing. The mesh was refined in the near-wall regions, where large velocity gradients were expected, resulting in a  $y^+ \sim 1$  at the walls. There was a negligible influence on the computations when the mesh density increased



**FIGURE 4: COMPUTATIONAL MODEL: (a) PERIODIC SECTOR WITH BOUNDARY TYPES, (b) CAVITY MESH, AND (c) GUIDE VANE AND BLADE MESHES**



**FIGURE 5: PURPOSE-BUILT LABORATORY RIG**

by a factor of 1.5. Thus, the solution was considered mesh independent with a cell count of approximately 6.6 million cells.

The simulations were performed using the compressible URANS solver in ANSYS Fluent. A first order implicit scheme was used for the temporal discretization and second order schemes were used for the spatial discretization of the governing equations. Turbulence was modelled using the shear-stress transport  $k-\omega$  model. For each time step of  $10^{-5}$  s, inner iterations were performed until the maximum residual reached  $10^{-6}$ . Mean quantities converged after a few shaft cycles. Simulations were performed with smooth and honeycomb end-walls for the baseline configuration, enabling a comparison between the numerically-predicted and experimental pressure distribution across the labyrinth seal. The honeycomb end-wall was used for the configuration with the FCC. The computational cost of a simulation was 1,600 and 4,000 core-hours per shaft cycle for the case with smooth and honeycomb end-walls, respectively.

The operating point of the cavity is defined by the pressure ratio across the cavity/blade, PR, and the swirl-ratio of the ingress into the upstream cavity,  $X_{k, in}$ . The full range of testing was in a design space  $1.05 < PR < 1.22$  and  $0.55 < X_{k, in} < 1.05$ . In the paper, we have presented detailed results at the design point,  $X_{k, in} = 0.8$  and  $PR = 1.08$ . Results at other operating points were qualitatively similar and measurements of improved torque were achieved across the full range. The swirl-ratio is defined in

Eq.2, where  $V_t$  is the tangential velocity component,  $\Omega$  is the rotor angular velocity, and  $b$  is the shroud radius. In the current work, the cavity was operated at  $PR=1.08$  and  $X_{k, in}=0.8$ . The rotational Reynolds number was  $Re_\phi = 1.6 \times 10^6$ .

$$X_k = \frac{V_t}{\Omega b} \quad (2)$$

## 2.2 Experiment

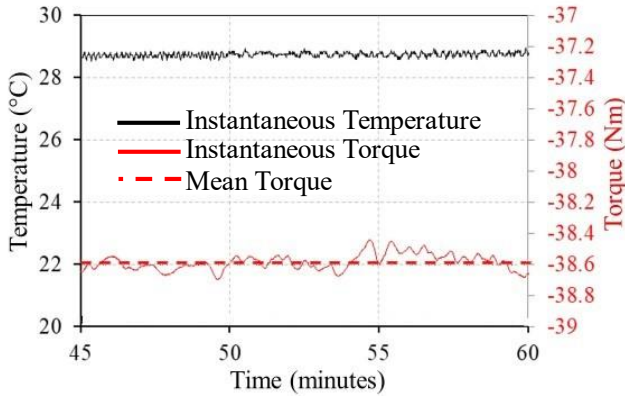
The cold-flow axial turbine rig at the University of Bath was used to conduct experiments simulating the flow paths in an LPT over-tip cavity at fluid-dynamically scaled conditions, as shown in Fig.5. The test facility is described in Jackson *et al.* [2] but adapted from a stator-well to an over-tip cavity configuration.

The cross-section view of the test section is also shown in Fig.5, which includes the new outer band annulus, stator, and rotor. The annulus features a row of 32 stator vanes (inlet guide vanes) and a row of rotor blades. The over-tip cavity is formed by the fins on the rotor shroud and the casing. The rotor is manufactured from three parts, with the hub fixed to the shaft by a hydraulic coupling. The rotor featured 33 blades – the number of which was deliberately different to the number of inlet guide vanes, in order to minimize the risk of harmonic effects. Flow into and out of the rotor-stator wheel-space was minimized by a labyrinth seal. The seal teeth were machined into the upstream rotor face and radially aligned with abradable Tufnol on the stator surface opposite. The test rig operating conditions are listed in Table 1. The test facility was deliberately designed to simulate the over-tip cavity flow in isolation, assessing windage losses in an engine-representative environment at low TRL. This was a proof-of-concept study using additive manufacturing technology to extend the design envelope.

The in-line torque meter (HBM T12) described by Jackson *et al.* [2] was used to measure the change in windage between the baseline honeycomb end-wall and the FCC. The sensor was re-calibrated in-situ over the larger torque range expected to be measured during the experiments (0 to -50 Nm). To isolate the change in cavity windage from the other torque contributions (e.g., bearing friction), a carefully controlled operating procedure was used for each test condition of  $X_{k, in}$ . As with the stator-well cavity experiments, the temperature of the bearing housing was closely monitored using a K-type thermocouple. A reference, steady-state temperature was found for the baseline

**TABLE 1: TEST RIG OPERATING CONDITIONS**

Parameter	Range	Design condition
$N$	0 → 6,000 rpm	4,000 rpm
$\dot{m}_A$	0 → 1.45 kg/s	~ 1.2 kg/s
$Re_\phi$	0 → $2.4 \times 10^6$	$1.6 \times 10^6$
$X_{k, in}$	0.55 → 1.05	0.8
PR	1.05 → 1.22	1.08



**FIGURE 6: TORQUE AND BEARING TEMPERATURE TRACE**

configuration over a small range of  $X_{k, in}$ . To ensure a fair torque comparison between the baseline and the FCC, the bearing temperature for the FCC experiments was closely matched to the reference baseline value (to within  $\pm 1$  °C). Once this value was reached, the test data was collected. At each value of  $X_{k, in}$ , the torque data was sampled over 30 s at a rate of 80 Hz. To minimize noise, a 1 Hz low-pass filter was used, and a median average of the sample taken. The stability of the bearing temperature and the torque is shown in Fig 6. for an example case. The uncertainty in the torque measurement is  $\pm 0.02$  Nm [2].

Although the cavity windage could not directly be measured, the change in windage was accurately determined. Since the other sources of torque were fixed using the preceding bearing warm-up method, the change in windage can be expressed non-dimensionally as a change in moment coefficient given by Eq. 3. Here,  $C_M$  is the rotor moment coefficient,  $M$  is the total measured torque,  $\rho$  is density,  $\Omega$  is rotor angular velocity, and  $b$  is the shroud radius. Note that the sign convention is for  $M$  to be positive in the direction of rotation – therefore, negative values indicate a windage torque, and positive values indicate that power is generated (work done by the fluid on the rotor).

$$C_M = \frac{M}{\frac{1}{2}\rho\Omega^2 b^5} \quad (3)$$

The remaining instrumentation for the pressure and swirl measurements are shown in Fig. 5. Static pressure taps were distributed in the main annulus across one vane pitch, upstream and downstream of the over-tip cavity. An axial distribution of pressure was also measured along the length of the over-tip cavity for the baseline and FCC configurations. The pressure drop across the rotor-stator labyrinth seal was monitored to ensure that the leakage remained minimal. The temperature near the labyrinth seal was measured to check that this did not exceed critical levels.

Gauge pressures were measured using four differential transducers (ESI PR3202) that were individually calibrated in-house. The transducers had a range of 0-400 mbar and an accuracy of  $\pm 0.3\%$  of the full-scale range ( $\pm 1.2$  mbar). Each

transducer was connected to a 48-channel Scani-valve system, allowing up to 192 pressure measurements to be made during a single experiment. The pressure data were acquired at 80 Hz and averaged over 2 s, following a settling period of a further 2 s.

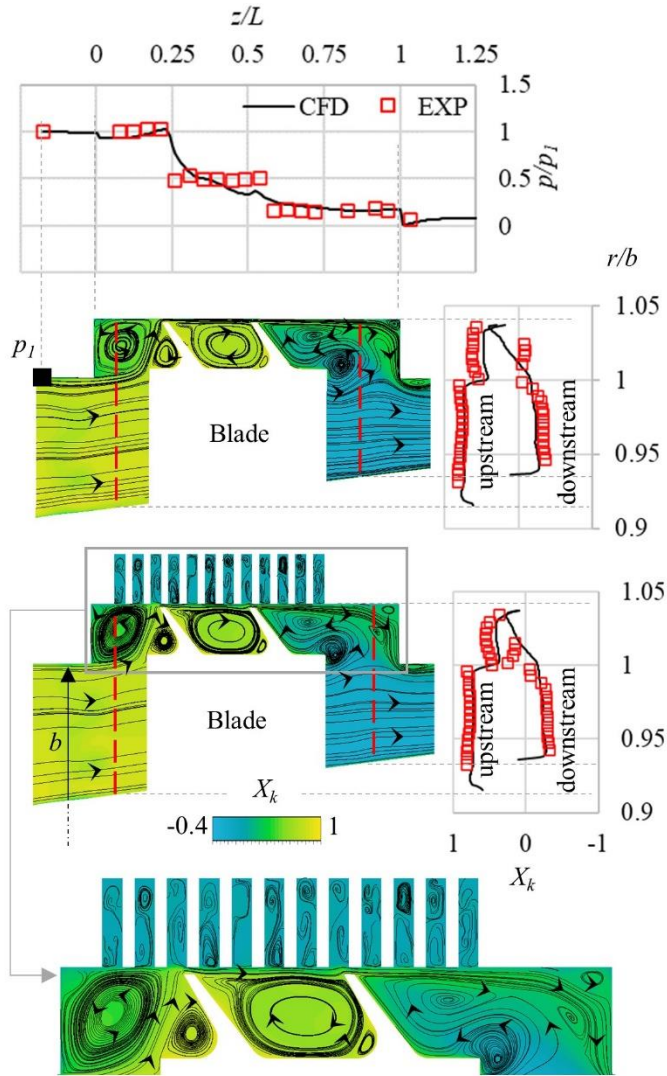
The local velocity components and corresponding flow angles in the upstream and downstream chambers of the tip cavity were determined using pressure measurements from the same custom drilled-elbow five-hole probe as that used for the stator-well experiments. The radial coordinate of the probe was controlled using a bespoke traversing system. Five separate differential transducers (“All Sensors” 5PSI-D-PRIME-MV, 345 mbar range) simultaneously acquired the pressures, sampled at 1000 Hz over a 5 s period before being averaged. Flow angles and velocities were then derived by applying the data to calibration coefficients. These coefficients were provided by Vectoflow, following their in-house calibration of the probe.

The five-hole probe was also used to measure the mid-annulus swirl at the upstream traversing location ( $r/b = 0.96$ ), when simultaneously collecting torque data. For these experiments, the probe pressure data was acquired at the same rate as the torque data (80 Hz) and averaged over the same sample period at each condition of  $X_{k, in}$ . This data was collected separately from that for the traversing experiments.

The flow control concepts were additively manufactured using stereolithography (SLA), printed by Laser Prototypes Europe Ltd with support on design for manufacture by Added Scientific Ltd. The synthetic printing material had a high stiffness to avoid deflection, with material properties that had similar characteristics to ABS/polypropylene. The FCCs were bonded together to form a ring, resulting in separate sub-assemblies, which could easily be interchanged in the rig.

### 3. BASELINE FLOW

Numerical and experimental results for the baseline configuration with smooth and honeycomb end-walls are shown in Fig.7. Note that the radial clearance between the teeth of the labyrinth seal and end-wall was identical for both cases. The contour plots in Fig.7 show the time-averaged and circumferentially-averaged swirl-ratio field from the numerical simulations. In-plane streamlines are superimposed on the contours to illustrate the predicted average flow structure in the axial-radial plane. The swirl-ratio field and flow structure are qualitatively similar for both end-walls. In the annulus, the swirl-ratio decreases from 0.8 to -0.4 as the flow passes through the blade row and generates power. The over-tip leakage flow enters the cavity near the upstream edge of the blade shroud, where it is subjected to the rotor pumping effect. It then passes between a recirculation zone on the stator side and a smaller recirculation zone on the rotor side before traversing the clearance of the labyrinth seal between the end-wall and a recirculation zone within the middle cavity. On exiting the seal, the leakage flow impinges on the radial wall of the downstream cavity and re-enters the main gas path. The leakage flow exits the downstream cavity on the stator side as egress. Low swirl-ratio fluid exiting the blade row is pumped up into the downstream cavity region between the rotor and leakage flow on the stator side as ingress.

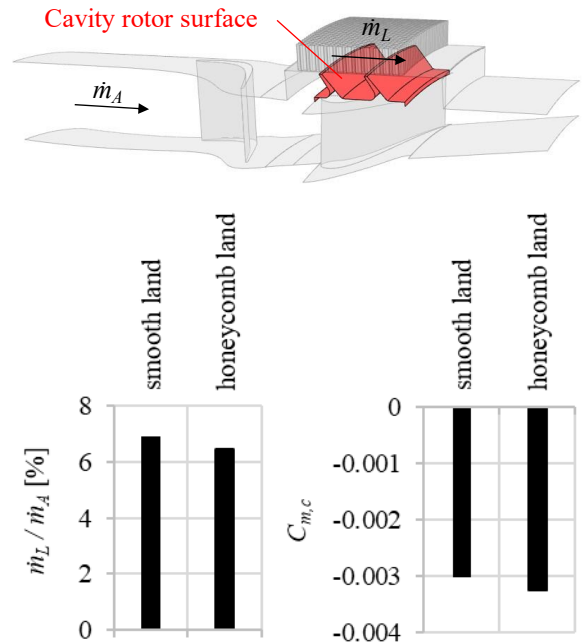


**FIGURE 7: PRESSURE AND SWIRL IN THE BASELINE SHROUD CAVITY FOR SMOOTH AND HONEYCOMB END-WALLS (PR = 1.08 and  $X_{k, in} = 0.8$ )**

376  
 377 In the case of the honeycomb end-wall, the leakage flow fills the  
 378 honeycomb cells with slow moving fluid that effectively  
 379 produces a momentum deficit for the leakage flow. This is  
 380 evident in the downstream cavity where there is an increased  
 381 angle of incidence between the leakage streamlines of the  
 382 leakage flow and the smooth section of end-wall downstream of  
 383 the honeycomb.

384 The radial distributions of swirl-ratio in Fig.7 are taken at  
 385 the two axial positions indicated by the vertical dashed lines on  
 386 the contour plots. These datum lines traverse the upstream and  
 387 downstream cavity/annulus. The numerical and experimental  
 388 distributions of swirl-ratio are qualitatively consistent. There are  
 389 quantitative discrepancies between simulation and experiment  
 390 inside the cavity, most notably in the downstream cavity of the  
 391 smooth end-wall. In general, the experimentally measured swirl-  
 392 ratio in the cavity is always of larger magnitude than the  
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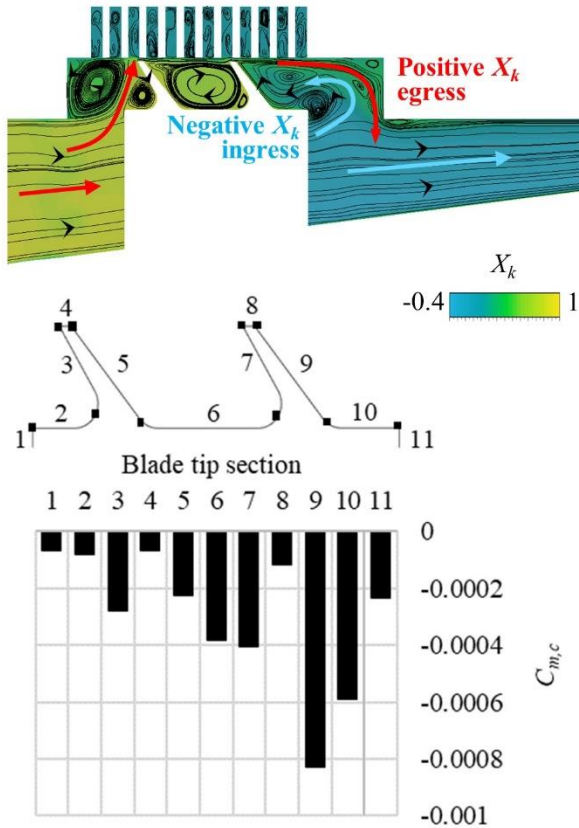
**FIGURE 8: NUMERICAL OVER-TIP LEAKAGE AND CAVITY WINDAGE FOR SMOOTH AND HONEYCOMB END-WALLS**

numerical prediction. This is believed to be due to the presence of an opening on the shroud in the case of the experiment that was necessary for the probe traverse to move in and out of the test section.

The pressure distribution across the labyrinth seal in Fig.7 is for the smooth end-wall and shows good agreement between simulation and experiment. Specifically, this confirms that the mass flow rate of the numerically predicted leakage is accurate as it will be proportional to the pressure drop across the seal. The uncertainty in the pressure readings outlined in Section 2 was used to determine the measurement uncertainty for  $p/p_1$ , as shown in the Appendix.

The influence of the honeycomb end-wall relative to a smooth casing was examined by numerical simulation. A comparison of the over-tip leakage mass flow rate and the cavity windage between the smooth and honeycomb end-walls is shown in Fig.8. The leakage mass flow rate is expressed as a percentage of the annulus mass flow rate and the cavity windage is expressed as a moment coefficient. Relative to the smooth end-wall, there is a lower leakage mass flow rate across the honeycomb case, but with increased cavity windage. The reduced axial flow velocity and mass flow through the seal is associated with the interaction with the honeycomb cells. The reduced tangential flow velocity results in a steeper velocity gradient at the rotor surface and hence increased windage.

The consistent validation with experiment was encouraging and the FCC was subsequently designed and developed through numerical simulation, as discussed in the next Section. The FCC was validated by experiment, with the results presented in Section 5.



**FIGURE 9: FLOW FIELD AND WINDAGE BREAKDOWN IN THE BASELINE SHROUD CAVITY**

#### 4. FLOW CONTROL CONCEPT

The flow control objective is twofold: (1) reduce the mixing loss generated where the leakage flow re-enters the main gas path downstream of the blade row, and (2) reduce windage loss from the over-tip cavity. The first step was to identify the flow features contributing to windage and mixing losses using the baseline geometry. A flow control strategy was then designed to mitigate the negative effects.

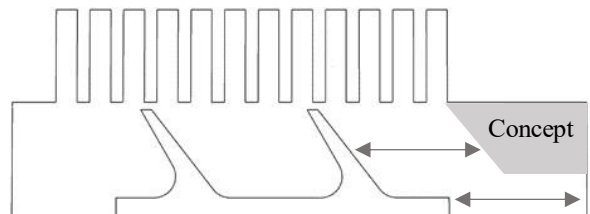
The schematic arrows on the swirl contour plot in Fig.9 show the cavity ingress and egress flows. The egress from the downstream cavity (marked positive  $X_k$  egress) enters the main gas path with a positive swirl-ratio and a strong component of radial velocity as it encounters the cavity wall. In contrast, the main gas path has a negative swirl-ratio and a negligible radial component. The resulting shear gives rise to mixing losses. Therefore, from the mixing loss perspective, the flow control strategy should reduce the radial component and the swirl-ratio of the egress from the downstream cavity.

The bar graph in Fig.9 shows a breakdown of the cavity windage. Each bar represents the moment coefficient on a section (marked 1 to 11) of the blade tip i.e., the rotating surfaces inside the cavity. A negative moment coefficient indicates that the moment is opposing the motion of the rotor. The bars in the graph are numbered to correspond to the numbered sections of the blade tip surface. The main contribution to the cavity

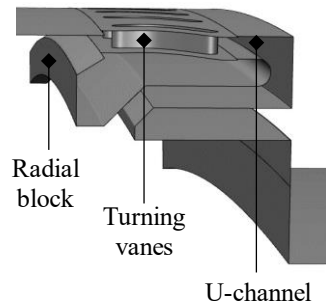
windage is from rotor surfaces 9-10, situated in the downstream cavity. This is not surprising as the swirl-ratio of the flow here was shown previously to be relatively low. The schematic arrows on the swirl-ratio contour plot indicate this is due to the negative  $X_k$  fluid exiting the blade row and being pumped radially into the downstream cavity. It is this ingress that is responsible for the large windage on sections 9-10. From the perspective of cavity windage, the flow control strategy should modify the flow topology to minimize downstream ingress.

Before a flow control strategy was devised to satisfy the aforementioned requirements, the positioning of the concept inside the cavity was also given due consideration. Restrictions were set by the Clean Sky 2 topic manager (industry partner), related to required rotor-stator clearances due to movement of components during transient operation and assembly stack-up uncertainty. The restricted design space is shown in Fig.10(a). Within these geometric constraints, the FCC shown in Fig.10(b) was devised to implement the flow control strategy shown in Fig.10(c). The concept is essentially a row of turning vanes in a U-shape channel. Windage is reduced by deflecting a portion of the over-tip leakage onto the rotor to create a recirculating region

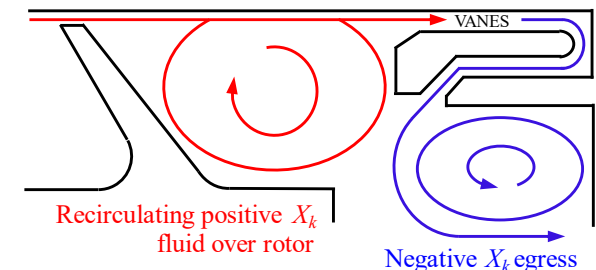
#### (a) Design space:



#### (b) Concept:

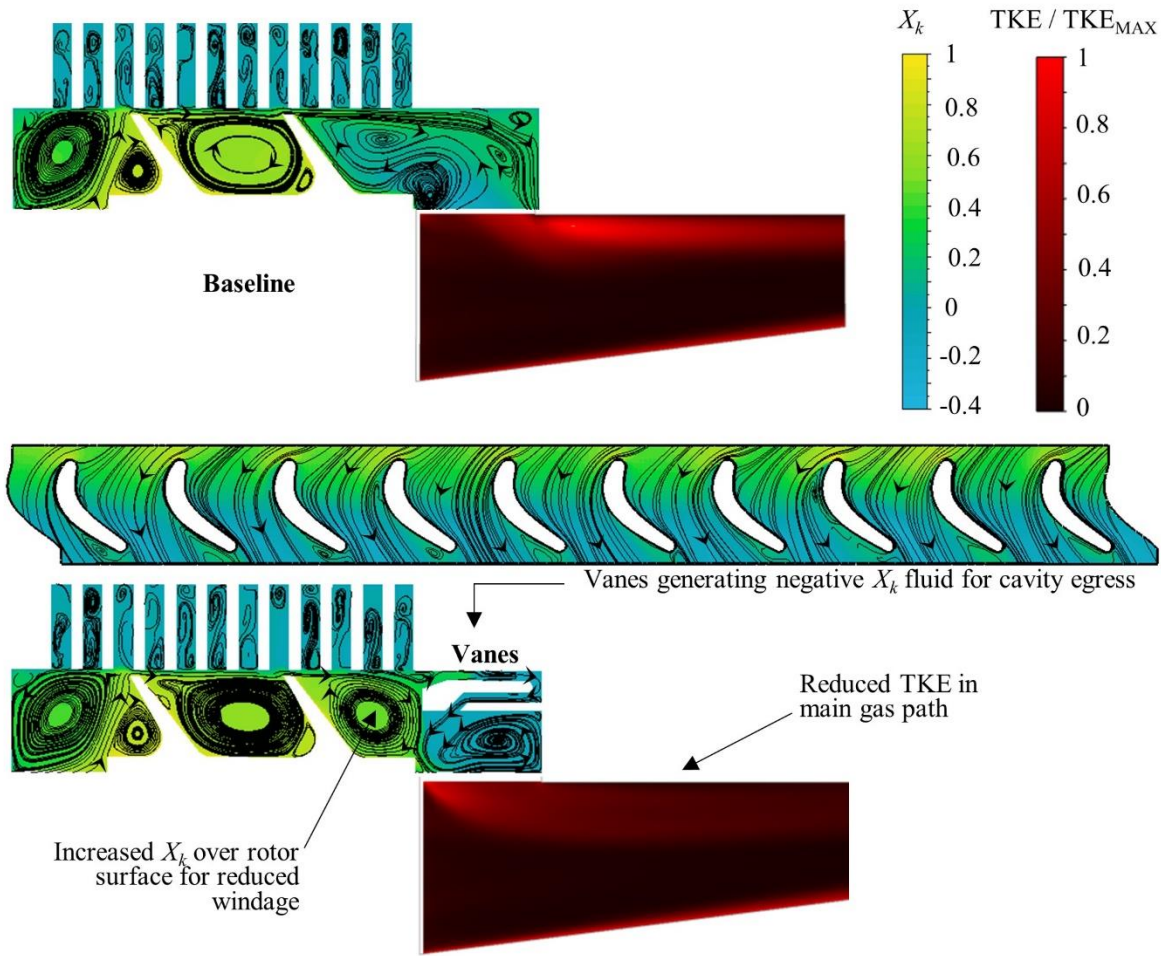


#### (c) Flow control strategy:



**FIGURE 10: FLOW CONTROL CONCEPT – THE DESIGN SPACE, FCC, AND FLOW CONTROL STRATEGY**





**FIGURE 11:** CONTOURS OF SWIRL-RATIO AND TURBULENT KINETIC ENERGY FOR BASELINE AND FCC CASES

474 of positive  $X_k$  fluid over the rotor surface. The portion of leakage 495  
 475 that is not deflected traverses the U-shape channel with the 496  
 476 turning vanes. The vanes turn the flow to better match the egress 497  
 477 swirl-ratio of the main gas path and the channel reduces the 498  
 478 component of radial velocity. The redirected leakage flow acts 499  
 479 to suppress the ingress of mainstream fluid pumped radially into 500  
 480 the over-tip cavity by the rotor. 501

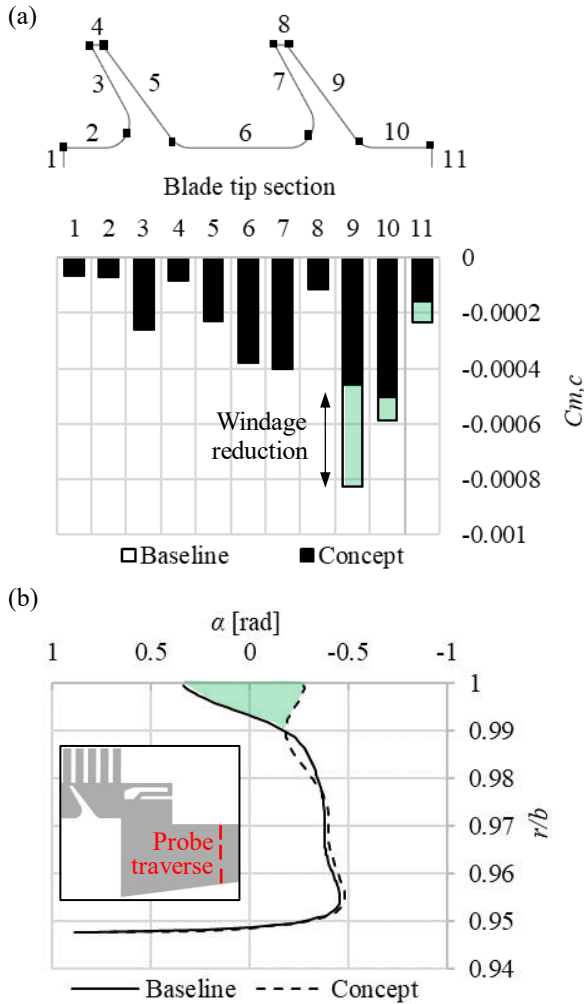
481 Numerical results from the simulations of the proposed 502  
 482 FCC and the baseline are shown in Fig. 11. The over-tip cavity 503  
 483 in both cases is shown with contours of time-averaged and 504  
 484 circumferentially-averaged swirl-ratio with superimposed in- 505  
 485 plane average streamlines. The streamlines show that the FCC 506  
 486 modifies the flow topology as intended. A portion of the leakage 507  
 487 flow exiting the labyrinth seal is deflected, forming a 508  
 488 recirculating region of positive  $X_k$  over the rotor surface; another 509  
 489 portion of the leakage flow traverses the U-shape channel, where 510  
 490 the turning vanes convert the positive swirl-ratio to a negative 511  
 491  $X_k$ , similar to that of the main gas path. 512

492 The flow through the turning vanes is also illustrated in 513  
 493 Fig.11, where the average  $X_k$  contours and streamlines are shown 514  
 494 at midspan. The leading-edge angle of the turning vanes (+55 515

degrees) was matched to the velocity angle of the oncoming  
 leakage flow, which was determined from the baseline flow. The  
 trailing-edge angle of the turning vanes (-23 degrees) was  
 matched to the velocity angle in the main gas path. Due to the  
 constrained design space in the axial direction (chord length =  
 16 mm), the velocity angle could not be matched at the trailing  
 edge without excessive camber, which was a limiting factor in  
 achieving better flow guidance through the vanes. The solidity  
 of the turning vanes was briefly investigated, and the flow was  
 found to be invariable beyond a solidity of unity.

The main gas path (or annulus) downstream of the blade is  
 shown in Fig.11 with contours of the average turbulent kinetic  
 energy (TKE). The TKE has been normalized using its  
 maximum value in the contoured region and is used to visualize  
 the mixing - shear leads to the generation of turbulence, that is  
 to the generation of turbulence kinetic energy. Relative to the  
 baseline, there is less TKE generated with the FCC and hence  
 reduced mixing loss.

The change of the moment coefficient on the blade tip  
 sections with the FCC included in the cavity is shown in  
 Fig.12(a). The moment coefficient for sections 9-11 becomes



**FIGURE 12:** COMPARISON OF THE CAVITY WINDAGE BREAKDOWN AND VELOCITY ANGLE DOWNSTREAM OF THE CAVITY BETWEEN BASELINE AND FCC

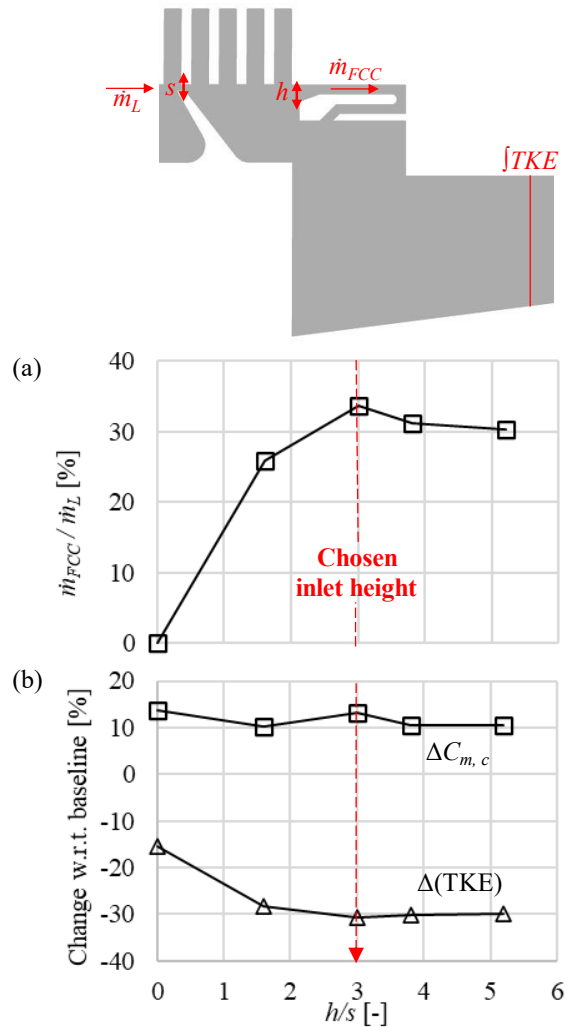
516 less negative when the FCC is included, with reduced windage  
 517 on the intended rotor surfaces. The cumulative reduction in  
 518 cavity windage is 16% relative to the baseline.  
 519

520 The velocity angle in the main gas path downstream of the  
 521 over-tip cavity for the baseline and FCC is shown in Fig.12(b).  
 522 The velocity angle is both time- and circumferentially-averaged.  
 523 The velocity angle in the near shroud region is better aligned  
 524 with that of the main gas path when the FCC is included, with a  
 525 more uniform distribution across the annulus. This improved  
 526 uniformity of velocity angle is consistent with the reduction in  
 527 generated TKE.

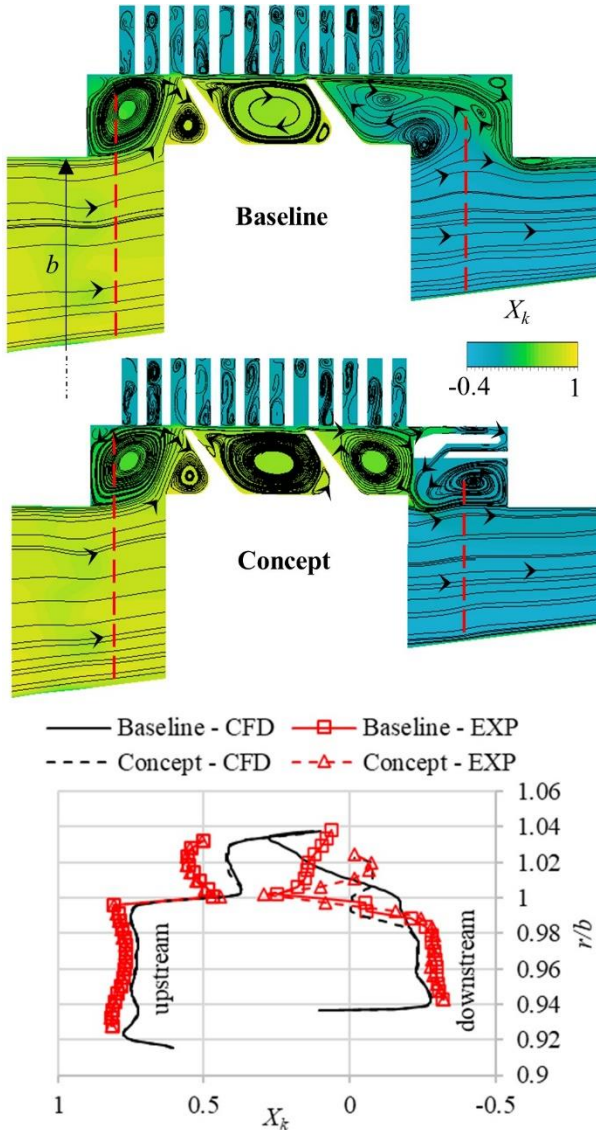
528 The channel inlet height of the FCC ( $h$  in Fig.13) was  
 529 optimized through a parametric study. The height controls the  
 530 proportion of fluid deflection relative to the amount passing  
 531 through the U-shape channel and influences the FCC  
 532 performance. The optimization was limited to the FCC inlet due  
 533 to the constrained design space in the radial direction and the  
 534 practical minimum-thickness requirements for additive  
 535 manufacture. The optimization process monitored the mass flow

536 rate through the FCC, the change in moment coefficient on the  
 537 blade tip relative to the baseline (i.e., the cavity windage  
 538 reduction), and the change of TKE in the main gas path  
 539 downstream of the cavity outlet relative to the baseline (i.e., the  
 540 TKE reduction). The TKE was integrated over a circumferential  
 541 cross-section of the periodic sector. The trends of these  
 542 parameters as a function of the FCC channel inlet dimension  
 543 ( $h/s$ ) are shown in Fig.13; here the inlet height,  $h$ , on the abscissa  
 544 is non-dimensionalized with respect to the minimum radial  
 545 clearance in the labyrinth seal,  $s$ . Simulations were performed for  
 546 the inlet heights  $h/s = 0$ ,  $h/s = 1.6$ ,  $h/s = 3.8$ , and  $h/s = 5.2$ . Note  
 547 that  $h/s = 0$  represents a fully blocked channel.

548 In Fig.13(a), the mass flow rate through the FCC is non-  
 549 dimensionalized with respect to the mass flow rate of the total  
 550 leakage flow. The mass flow rate through the FCC is seen to  
 551 increase as the inlet height increases, as would intuitively be  
 552 expected. The mass flow becomes invariable for  $h/s > 3$ .  
 553 The variation of cavity windage reduction,  $\Delta C_{m,c}$ , and TKE  
 554 reduction with  $h/s$  are shown in Fig.13(b). Note that the windage



**FIGURE 13:** OPTIMIZATION OF FCC — PERFORMANCE WITH RESPECT TO INLET HEIGHT



**FIGURE 14:** COMPARISON OF NUMERICAL AND EXPERIMENTAL SWIRL-RATIO DISTRIBUTIONS BETWEEN BASELINE CAVITY AND CAVITY WITH CONCEPT

556 torque is negative when it is against the direction of rotation and  
 557 therefore a positive  $\Delta C_{m,c}$  indicates a reduction in cavity windage  
 558 torque. It is instructive to observe these variations in conjunction  
 559 with the variation in mass flow rate. The cavity windage  
 560 reduction remains stable as the mass flow rate through the  
 561 concept increases. This indicates that although the amount of  
 562 fluid recirculating over the rotor is decreasing as  $h/s$  increases,  
 563 there is no significant ingestion of negative  $X_k$  fluid. Hence, this  
 564 suppression of ingestion remains effective even when there is a  
 565 minimum amount of leakage flow being recirculated. In contrast,  
 566 the beneficial reduction in TKE increases with increasing mass  
 567 flow rate through the FCC because the amount of egress fluid  
 568 (with negative  $X_k$ ) being supplied to the annulus is increasing. It  
 569 is helpful to reiterate that the FCC splits the leakage flow into  
 570 two portions: part of the flow passes through the FCC and is  
 571

572 converted to the swirl-ratio of the main gas path, while the swirl-  
 573 ratio of the recirculated portion is not converted. Ultimately, the  
 574 total leakage flow rate will exit the cavity. Hence, the greater the  
 575 proportion that traverses the FCC to better match the  $X_k$  of the  
 576 main gas path, the more favorable will be the outcome in terms  
 577 of annulus TKE reduction.

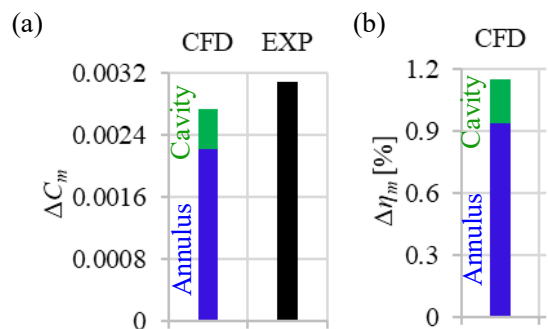
578 The parametric study shows that an inlet height  $h/s = 3$  is  
 579 sufficient to achieve an optimum FCC performance – there is no  
 580 benefit beyond this point, and this was the chosen inlet height.

581 The FCC, after being developed and optimized through  
 582 numerical simulation, was then created physically using an  
 583 additive manufacturing process and installed in the experimental  
 584 rig for testing and validation.

## 5. VALIDATION

585  
 586 The numerical prediction for the performance of the FCC  
 587 was validated against experimental measurement: first, the  
 588 distribution of swirl-ratio upstream and downstream of the blade;  
 589 and second, the change in rotor windage torque between baseline  
 590 and FCC. The former comparison assesses whether the resulting  
 591 flow topology forms as intended, and the latter comparison  
 592 assesses the accuracy of the combined reduction of the windage  
 593 and mixing losses. It is important to recognize that the influence  
 594 of the FCC on mixing loss generates a change in the windage for  
 595 the rotor blade: a change in the velocity angle downstream of the  
 596 blade results in a change of the flow at the shroud of the blade.  
 597 Thus, the rotor windage torque provides a measure of the  
 598 combined reduction of cavity windage and mixing losses.

600 The radial variation of swirl-ratio upstream and  
 601 downstream of the blade for both the baseline and FCC  
 602 configurations are shown in Fig.14. These distributions of  $X_k$   
 603 were taken along the dashed datum lines superimposed on the  
 604 contour maps. Here,  $X_k$  is both time- and circumferentially-  
 605 averaged. The in-plane average streamlines have also been  
 606 superimposed. The blade shroud is located at  $r/b = 1$ . The  
 607 numerical and experimental distributions of  $X_k$  are qualitatively  
 608 similar, with some quantitative discrepancies inside the over-tip  
 609 cavity ( $r/b > 1$ ). While the upstream swirl-ratio distribution is  
 610 identical for the baseline and FCC cases, there are significant  
 611 differences in the downstream distribution inside the cavity and  
 612 in the near cavity region of the annulus. Hence, the FCC has



**FIGURE 15:** CHANGE IN MOMENT COEFFICIENT AND MECHANICAL EFFICIENCY BETWEEN BASELINE AND FCC

614 influenced the swirl-ratio distribution in the intended region, as 665  
 615 expected. The main region of influence is  $1.02 > r/b > 0.98$ , 666  
 616 where  $X_k$  for the FCC changes relative to the baseline. The 667  
 617 contour plots (with the in-plane streamlines) show this region is 668  
 618 influenced by egress from the cavity. In the baseline flow, the 669  
 619 cavity egress occurred further downstream near the cavity end- 670  
 620 wall, but the change in topology with the FCC has moved the 671  
 621 egress upstream. This feature is also captured experimentally - 672  
 622 despite some quantitative discrepancy, there is good qualitative 673  
 623 consistency with the simulation. 674

624 The comparison between the numerically predicted and the 675  
 625 experimentally measured change in rotor windage due to the 676  
 626 FCC is shown in Fig.15(a). The change is expressed in terms of 677  
 627 a moment coefficient. The numerical result has been 678  
 628 decomposed into the fraction from the rotor surface inside the 679  
 629 cavity (i.e., due to the blade tip), and the fraction from the rotor 680  
 630 surface inside the annulus (i.e., the blade). The predicted change 681  
 631 in rotor windage is in good agreement with the experiment —the 682  
 632 numerical prediction is consistent within 10% of the 683  
 633 experimental measurement. The breakdown of the numerical 684  
 634 result shows that the main contribution to the change in moment 685  
 635 coefficient is from the annulus. This is due to the improved flow 686  
 636 around the blade as a result of the FCC producing a velocity 687  
 637 angle near the blade shroud that is better aligned with the blade’s 688  
 638 flow exit angle. 689

639 The change in mechanical efficiency due to the change in 690  
 640 rotor windage torque is shown in Fig.15(b). Mechanical 691  
 641 efficiency is calculated using Eq.4 [18], which is the ratio of the 692  
 642 output mechanical energy to the isentropic change in enthalpy 693  
 643 across the turbine stage. In Eq.4,  $\eta_m$  is mechanical efficiency,  $M$  694  
 644 is the rotor moment torque,  $\Omega$  is the rotor angular velocity,  $\dot{m}_A$  is 695  
 645 the annulus mass flow rate,  $C_p$  is the specific heat capacity of air 696  
 646 at constant pressure,  $T_{in}$  is the total temperature at the stage inlet, 697  
 647  $P_{in}$  is the total pressure at the stage inlet, and  $P_{out}$  is the total 698  
 648 pressure at the stage outlet. The FCC increases the mechanical 699  
 649 efficiency of the turbine stage by 1%. Note that this calculation 700  
 650 is for the stage in isolation and does not account for the influence 701  
 651 of the changes of the flow on the downstream stages. 702  
 652

$$\Delta\eta_m = \frac{\Delta M \cdot \Omega}{\dot{m}_A C_p T_{in} \left[ 1 - \left( \frac{P_{out}}{P_{in}} \right)^{\frac{\gamma-1}{\gamma}} \right]} \quad (4)$$

## 653 6. PRACTICAL IMPLICATIONS

654 The key contributions and innovations of this study are  
 655 summarized here. This research was a response to the EU Clean  
 656 Sky 2 programme, exploring the use of additive manufacturing  
 657 (AM) for flow control devices to reduce windage torque in LPT  
 658 over-tip leakage cavities. Numerical simulation was used to  
 659 create a flow-control concept, which was subsequently  
 660 manufactured using AM and tested in an engine-representative  
 661 test rig at low TRL. From a practical perspective, scaling to the  
 662 engine would only be strictly appropriate for the geometry used  
 663 in the experiments and subject to the limits of dimensional  
 664 similitude. We would expect engine designers to validate their

CFD codes on the experimental rig conditions and extrapolate to  
 higher Mach numbers and Reynolds numbers. However, the  
 proof-of-concept would be valid and can be implemented into  
 the engine design process. The research has extended the design  
 envelope for AM technology and provided a potential prototype  
 appropriate for an engine demonstrator at higher TRL.

## 7. CONCLUSION

A joint numerical and experimental campaign has  
 introduced an optimized flow control concept (FCC) to reduce  
 both the windage torque and the mixing losses in an LPT over-  
 tip cavity. The FCC was a device incorporating a row of turning  
 vanes in the downstream chamber of the cavity; the device  
 redirected positively swirling flow onto the downstream face of  
 the rotor fin to reduce the windage, while the incorporated vanes  
 turned the over-tip leakage in the direction of the main annulus  
 flow to minimize mixing losses. The concept was optimized to  
 perform effectively with an engine-representative honeycomb  
 end-wall at cruise flight conditions.

The experiments were conducted in a cold-flow axial  
 turbine rig, which simulated the flow paths in an LPT over-tip  
 cavity at fluid-dynamically scaled conditions. An in-line torque  
 meter was used to measure the change in windage between the  
 baseline honeycomb end-wall and the FCC. Radial distributions  
 of swirl-ratio were measured using a five-hole probe at two axial  
 positions upstream and downstream of the over-tip cavity and  
 annulus. The numerical and experimental distributions of swirl-  
 ratio were qualitatively consistent, showing the FCC operated as  
 designed.

There was less computed turbulent kinetic energy generated  
 with the FCC (relative to the baseline) and consequently reduced  
 mixing loss, providing further confidence in the flow control  
 strategy. Experiments and computations were consistent with a  
 cumulative reduction in cavity windage of 16%. The FCC is  
 estimated to increase the mechanical efficiency of the turbine  
 stage in isolation by 1%. It is expected the FCC will be tested at  
 higher TRL in an engine demonstrator.

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## NOMENCLATURE

LPT	Low-pressure turbine
FCC	Flow control concept
$b$	Shroud radius
$U$	Rotor speed
$N$	Rotor speed in revolutions per minute
rpm	Revolutions per minute
$M$	Torque

720	$\Omega$	Rotor angular velocity
721	$V_t$	Tangential flow velocity
722	$X_k$	Swirl-ratio
723	$X_{k, in}$	Swirl-ratio of cavity ingress
724	PR	Pressure ratio
725	$p$	Static pressure
726	$p_l$	Static pressure upstream of cavity
727	$z$	Axial coordinate
728	$L$	Cavity length
729	$\dot{m}_A$	Annulus mass flow rate
730	$\dot{m}_L$	Leakage mass flow rate
731	$\dot{m}_{FCC}$	Through-concept mass flow rate
732	$C_{m, c}$	Cavity moment coefficient
733	$C_m$	Rotor moment coefficient
734	$Re_\phi$	Reynolds number
735	$\alpha$	Velocity angle
736	$s$	Seal clearance
737	$h$	Concept inlet height
738	TKE	Turbulent kinetic energy
739	$C_P$	Air heat capacity at constant pressure
740	$\gamma$	Air heat capacity ratio
741	$P_{in}$	Total pressure at inlet of turbine stage
742	$P_{out}$	Total pressure at outlet of turbine stage
743	$T_{in}$	Total temperature at inlet of turbine stage
744	$\eta_m$	Mechanical efficiency of turbine stage

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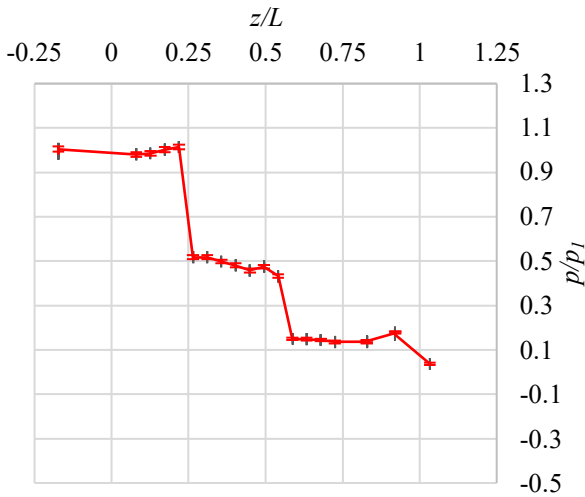
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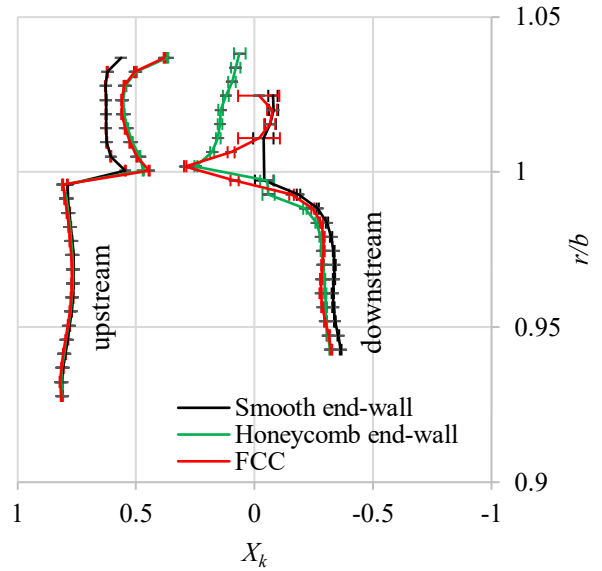
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840  
 841 **APPENDIX**  
 842 The uncertainty in the pressure measurements across the  
 843 over-tip in Figure 7 is shown in Figure 16 below. The transducers  
 844 had a range of 0-400 mbar and an accuracy of  $\pm 0.3\%$  of the full-  
 845 scale range ( $\pm 1.2$  mbar).



**FIGURE 16:** EXPERIMENTAL PRESSURE MEASUREMENTS ON THE SMOOTH END-WALL SHOWING MEASUREMENT UNCERTAINTY FOR DATA IN FIGURE 7

846  
 847 The local velocity components and corresponding angles of  
 848 the flow upstream and downstream of the tip cavity were  
 849 determined using pressure measurements from a custom five-  
 850 hole probe (manufactured by Vectoflow GmbH). Flow angles  
 851 and velocities were derived by applying the data to calibration  
 852 coefficients provided by Vectoflow [19], following their in-  
 853 house calibration of the probe. Flow angles are accurate to  $< \pm$   
 854  $1^\circ$ , though Ruchala et al. [20] state the accuracy to be  $< \pm 0.2^\circ$ .  
 855 The uncertainty in velocity depends on the range of the pressure  
 856 scanner, which in this case was 345 mb. Figure 17 shows the  
 857 uncertainty on the swirl measurements for all the tested  
 858 configurations.



**FIGURE 17:** UPSTREAM AND DOWNSTREAM EXPERIMENTAL VARIATION OF  $X_k$  WITH RADIUS SHOWING MEASUREMENT UNCERTAINTY FOR DATA PRESENTED IN FIGURES 7 AND 14

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