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DOI: [10.1016/j.jmmm.2018.03.054](https://doi.org/10.1016/j.jmmm.2018.03.054)

Document Version Publisher's PDF, also known as Version of record

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Citation for published version (APA):

Devonport, A., Vishina, A., Singh, R. K., Edwards, M., Zheng, K., Domenico, J., Rizzo, N. D., Kopas, C., van Schilfgaarde, M., & Newman, N. (2018). Magnetic Properties of chromium-doped Ni Fe thin films. JOURNAL<br>OF MAGNETISM AND MAGNETIC MATERIALS, 460, 193-202, https://doi.org/10.1896/i3mmm.2018.03.054 OF MAGNETISM AND MAGNETIC MATERIALS, 460, 193-202.<https://doi.org/10.1016/j.jmmm.2018.03.054>

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#### [Journal of Magnetism and Magnetic Materials 460 \(2018\) 193–202](https://doi.org/10.1016/j.jmmm.2018.03.054)

### Journal of Magnetism and Magnetic Materials

journal homepage: [www.elsevier.com/locate/jmmm](http://www.elsevier.com/locate/jmmm)



### Research articles

## Magnetic properties of chromium-doped  $Ni_{80}Fe_{20}$  thin films

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#### article info

Article history: Received 10 November 2017 Received in revised form 28 February 2018 Accepted 22 March 2018 Available online 27 March 2018

#### abstract

This paper investigates the properties of thin films of chromium-doped  $Nis_0Fe_{20}$  (Permalloy) that could potentially be useful in future low-power magnetic memory technologies. The addition of chromium reduces the saturation magnetization,  $M_s$ , which is useful for low-energy switching, but does not significantly degrade the excellent switching properties of the host material even down to 10 K, the lowest temperature measured, in films as thin as 2.5 nm. As an example, an alloy film composed of 15% chromium and 85% Ni<sub>80</sub>Fe<sub>20</sub> has an M<sub>s</sub> just over half that of pure Ni<sub>80</sub>Fe<sub>20</sub>, with a coercivity H<sub>c</sub> less than 4 Oe, an anisotropy field H<sub>k</sub> less than 1 Oe, and an easy-axis remanent squareness  $M_r/M_s$  of 0.9 (where  $M_r$  is the remanent magnetization). Magnetodynamical measurements using a pulsed inductive microwave magnetometer showed that the average Landau Lifshitz damping  $\lambda$  was relatively constant with changing Cr content, but increased significantly for thinner films ( $\lambda \approx 150$  MHz for 11 nm,  $\lambda \approx 250$  MHz for 2.5 nm), and at low bias fields likely due to increased magnetic dispersion. Density functional theory calculations show that chromium reduces  $M<sub>s</sub>$  by entering the lattice antiferromagnetically; it also increases scattering in the majority spin channel, while adding almost insignificant scattering to the minority channel.

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#### 1. Introduction

Ferromagnetic materials have been used for over one hundred years to store information. Early computer memory stored information in magnetic ceramic rings (ferrite core memory), on ferromagnetic coating of cylinders (drum memory) and on discs (floppy discs and hard drives). In the latest stages of memory development, it has become clear that patterning the magnetic materials into bits can enhance the density of magnetic memory storage systems (bitpatterned media)  $[1-7]$ . As capacity and speed improve, it has become apparent that such high performance memories used in personal computers, data centers and supercomputers can consume  $\sim$ 10% [\[8\],](#page-10-0)  $\sim$ 25% [\[9\]](#page-10-0) and  $\sim$ 33% [\[10,11\]](#page-10-0) of a system's power, respectively.

One way to decrease the power consumed by write operations is to substitute materials with smaller M<sub>s</sub>. The Stoner-Wohlfarth model, which describes single-domain coherent magnetization rotation of a patterned bit, predicts an energy barrier from shape anisotropy that scales as  $E_b \propto M_s^2 t^2$ , where t is the film thickness [\[12,13\]](#page-10-0). A material with low  $M_S$  could be used to reduce write power, in principle, in a number of recently-developed technologies, including bit patterned media [\[7\]](#page-10-0), conventional field-switched magnetic random-access memory (MRAM) [\[2\],](#page-10-0) spin-torque MRAM [1], Josephson MRAM (JMRAM) [\[3–5\]](#page-10-0) and nanomagnetic memory  $[6]$ . The minimum usable  $M_s$  is limited by the need to maintain large enough energy barrier to prevent data loss due to thermal fluctuations. [\[14,15\]](#page-10-0). Since JMRAM will operate at a temperature of 4 K only, low  $M_s$  alloys are of particular interest for this application.

In addition to choosing low-M<sub>s</sub> material, for applications one also needs a high quality film with minimal magnetic defects to produce optimum device operation. Extrinsic factors such as compositional inhomogeneity, structural defects and rough topographies, can increase the magnetic switching variations in arrays of patterned bits to the point where write programming error rates become unacceptably high.

The desired magnetic properties to demonstrate high quality in a continuous magnetic thin film having an intrinsic anisotropy  $H_k$ are a low coercivity H<sub>c</sub> and high remnant squareness (Sq =  $M_r/M_s$ ) in the easy axis direction, and a low squareness in the hard axis direction. A small magnetostriction is also preferred to minimize the influence of grain orientation and stress on switching properties. Small magnetodynamic damping is also desirable, both for





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<https://doi.org/10.1016/j.jmmm.2018.03.054> 0304-8853/ 2018 The Authors. Published by Elsevier B.V.

low power switching using spin torque [1], and also because a large damping can often indicate a large extrinsic contribution from magnetic defects which can inhibit or increase variability in switching at high speeds.

The operation and performance of magnetoelectronic devices can also depend on the transport properties through the ferromagnetic layers. For example, giant magnetoresistive memory (GMR) devices can require a large disparity between the minority and majority mean free paths, whereas JMRAM devices need both types of carriers to traverse the magnetic layers with minimal spin-flip scattering that will destroy the superconducting Cooper pairs [\[16\].](#page-10-0)

In order to minimize the switching energy, all these desirable properties need to be maintained down to film thicknesses as small as a few nanometers. Since JMRAM devices operate at cryogenic temperatures, the magnetic switching properties must also be retained down to low temperature (i.e. 4 K). Some of the other devices applications mentioned earlier may also benefit from low temperature operation in order to reduce their write energies. This possibility arises as a direct consequence of the reduced thermal activation relaxing the magnetic bit's thermal stability require-ment for data retention [\[17\].](#page-10-0) With this in mind, we have characterized the properties of the thin films in this study over a wide range of temperatures.

The  $Ni_{80}Fe_{20}$  alloy (Permalloy) commonly employed in memory applications satisfies the requirement for low  $H_c$ , near-zero magnetostriction and simultaneous near-zero magnetocrystalline anisotropy, and low intrinsic  $H_k$ , even at cryogenic temperatures. However,  $Ni_{80}Fe_{20}$  has a high  $M_s$ , and a somewhat small minority carrier mean free path. Previous work has shown that the  $M_s$  of Ni-Fe alloys could be reduced with smaller amounts of Cr dopant compared to more commonly used dopants like Mo or Cu [\[18\].](#page-10-0) Therefore, we examined reducing  $M_s$  in  $N_{80}Fe_{20}$  by adding chromium. We found that  $Ni_{80}Fe_{20}$  diluted with chromium can be a low M<sub>s</sub> ferromagnetic material with excellent magnetic properties over a range of temperatures (10–300 K) and thicknesses of interest to the device community (i.e. 2.5–11 nm). Our study shows that an alloy content of up to  $\sim$  15% Cr attains very desirable properties, including a reduced M<sub>s</sub> of  $\approx$  400 emu/cm<sup>3</sup>, an H<sub>c</sub> of  $\approx$ 4 Oe, an H<sub>k</sub> of  $\approx$ 1 Oe, and a squareness of  $\approx$  0.9, which are maintained even down to cryogenic temperatures. The magnetodynamic damping is not significantly affected by the addition of Cr. Density functional theory (DFT) calculations using the coherent potential approximation indicate that diluting  $N<sub>80</sub>Fe<sub>20</sub>$  with Cr diminishes the majority mean free path from 6.0 nm to 0.35 nm, while it does not significantly affect the minority mean free path of 0.35 nm.

Earlier studies by Fassbender [\[20\]](#page-10-0) and Folks [\[21\]](#page-10-0) of Ni-Fe-Cr alloys formed the material using ion implantation of Cr, and found that both the Curie temperature  $T_c$  and  $M_s$  were reduced from that of  $\text{Ni}_{80}\text{Fe}_{20}$  at room temperature. Unfortunately, the use of implantation to form the alloy makes it difficult to distinguish which magnetic properties are due to the intrinsic properties of Cr doping and which are influenced by the implant-induced defects. The structural properties of 2  $\mu$ m thick films [\[22\]](#page-10-0) and the magnetic damping properties of 25 nm films [\[23\]](#page-10-0) of this alloy have also been investigated.

#### 2. Methods

Thin films of composition  $Nb/Ru/(Ni_{80}Fe_{20})_{100-x}Cr_x/Ru/Nb$  were deposited at room temperature onto thermally oxidized Si (1 0 0) wafers using magnetron sputter guns (Meivac Inc., Sunnyvale, CA) at 3 mTorr Ar pressure in an unbaked UHV chamber with a base pressure of less than  $5 \times 10^{-8}$  Torr. (Ni<sub>80</sub>Fe<sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> films were grown on a stack of 5 nm of Nb and 2 nm of Ru seed layer to obtain lower coercivity  $(H_c)$  and higher remanent squareness  $(Sq = M_r/M_s)$  in the magnetic film [\[24\].](#page-10-0) Magnetic films were capped with 2 nm Ru/5 nm Nb to act as a cap to avoid oxidation or other contamination reaching the ferromagnetic layers. The Ni $_{80}$ Fe  $_{20}$ was deposited at 15 W power at normal incidence to the substrate, while the Cr target was positioned at a  $45^{\circ}$ angle from the substrate. The power levels of the Cr sputter gun were adjusted from 2 to 30 W in order to attain a growth rate of  $\sim$ 0.2 nm per second and the desired Cr concentration in the film. The films were deposited in a static magnetic field at the substrate of  $H \sim 50$  Oe to induce an intrinsic uniaxial anisotropy  $H_k$  from pair ordering and an easy axis magnetization direction parallel to the field. Samples used for measuring magnetic, transport and chemical properties were fabricated to thicknesses of 2.5 nm, 11 nm, and 50 nm, respectively. One film was grown for each combination of thickness and Cr content. The film thicknesses were determined using Rutherford Backscattering Spectrometry.

Quasistatic switching properties at 300 K and 10 K (just above the critical temperature of the base Nb layer) were obtained from M-H loops measured using a Quantum Design Physical Property Measurement System equipped with a vibrating sample magnetometer (VSM). The oven option for this instrument, capable of heating the samples to 1000 K, was used to measure Curie temperatures  $T_c$ . To characterize the low-temperature properties, a temperature of 10 K was chosen so that the diamagnetic property of the Nb's superconducting state at less than 9.2 K did not influence the magnetic measurement results.

Magnetodynamic switching properties, including  $M_s$ , ferromagnetic resonance (FMR) frequency,  $f_p$  decay time  $\tau_p$ , and anisotropy field  $H_k$ , were measured using a pulsed inductive microwave magnetometer (PIMM) [\[25,26\].](#page-10-0) The electrical resistivities of the films were measured using an inline 4-point probe mounted on a dipping stick that was inserted into a liquid He Dewar. Highresolution  $\theta$ -2  $\theta$  coupled-scan X-ray diffraction (PANalytical X'Pert PRO with the curved X-ray mirror optics configuration) were used to measure lattice constants and to identify the primary and secondary phases in the films. The incident beam was conditioned using a parabolic MRD mirror with a  $\frac{1}{4}$  degree fixed divergence slit, no anti-scatter slit, and 10 mm fixed mask. The diffracted beam optics used a parallel plate collimator at 0.09. Two representative  $\theta$  -2  $\theta$  scans, showing the (Ni<sub>80</sub>Fe<sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> (1 1 1) peak near  $2 \theta = 44^{\circ}$ , are shown in Fig. 1.



Fig. 1. Representative X-ray diffraction  $\theta$  -2 $\theta$  scans of two (Ni<sub>80</sub>Fe<sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> films, showing the  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  (1 1 1) peak near 44°.

Density functional electronic structure calculations were performed to analyze the electrical and magnetic properties of the  $(Ni_{80}Fe_{20})_{1-x}Cr_{x}$  alloys. We employed a Green's function formalism within the local-density approximation (LDA), using the tightbinding linear muffin tin orbital (LMTO) basis and atomic sphere approximation (ASA); alloys are described within the coherent potential approximation (CPA) [\[27\].](#page-10-0) The alloy yields a complex, dynamical self-energy  $\Sigma(\omega)$  which supplies information about alloy contribution to electron and spin scattering. In particular the imaginary part of  $\Sigma$  at the Fermi level ( $\omega$ =0) is directly proportional to the inverse scattering lifetime. For additional details on the method and analysis, see Ref. [\[19\].](#page-10-0)

#### 3. Results and discussion

#### 3.1. Structural properties

A previous study of the phases of Ni-Fe-Cr films [\[22\]](#page-10-0) found that a single FCC phase is thermodynamically stable for all alloy compositions used in this study. For the  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  films in this study, the lattice constants obtained from the  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  $(1 1 1)$  Bragg diffraction peaks are shown in Fig. 2. The lattice constant increased in a near linear fashion with the addition of Cr, indicating that Cr is entering substitutionally into the  $Ni_{80}Fe_{20}$  lattice over this range of doping.

The significant increase in lattice constant with increasing Cr content is expected, given the general trend for Cr to have a larger ''typical" metallic radii in a 12 nearest neighbor face-centeredcubic arrangement (1.28 Å) when compared to that of Ni (1.24  $\AA$ ) and Fe (1.26  $\AA$ ) [\[28\].](#page-10-0) However, density functional calculations find that the magnetic interactions significantly influence the lattice constant. Total energy CPA calculations were as a function of lattice constant for 0 and 20% Cr concentrations for both magnetic and nonmagnetic  $(Ni_{80}Fe_{20})_{1-x}$  Cr<sub>x</sub>. These results showed that the magnetic pressure originating from the change in the magnetic energy with respect to volume plays an important role in determining the lattice constant. For the non-magnetic case the minimum-energy lattice constant changes from 3.478 to 3.493 Å, a change of 0.5%, close to the measured change in Fig. 2. For the magnetic case the corresponding numbers are 3.504 Å and 3.509 Å, much smaller than the observed change. From this we can conclude that the volume-dependence of the lattice constant

0.356 attice Constant (nm) 0.355 0.354 0.353  $\Omega$ 5 10 20 25 30 35 40 15 % Cr (mole frac.)

Fig. 2. Dependence of lattice parameter on Cr content in  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  layers. Lattice parameter values are obtained from (1 1 1) Bragg reflection peaks at  $\sim$ 44°. Uncertainty of the lattice parameters is no greater than ±0.0001 nm. This uncertainty was inferred from the accuracy to which the standard Si substrate (4 0 0) peak was measured using the X-ray mirror optics in the same measurement scans. Fig. 3. Dependence of local moments on the concentration x in  $(N_{\text{iso}}Fe_{20})_{1-x}Cr_x$ .

above the Curie temperature is quite different from what happens at cryogenic temperatures. It is difficult to assess what the magnetic effect would be at room temperature. In the LDA, the system is already paramagnetic there, contrary to experiment, so to correctly describe the change in lattice constant with temperature requires a beyond LDA theory. We can reasonably expect the nonmagnetic and magnetic LDA results to bracket the measured results at room temperature. In fact, the nonmagnetic calculations are close to the experiment. Whether this is a fortuitous accident or already at room temperature the magnetic energy of the real systems is already small, is difficult to determine. This will depend on the how the local moments change with temperature as a function of concentration. Fig. 3 shows the local moments at 0 K projected onto the atomic sites. The small moments on Ni and Cr are very likely rapidly quenched as temperature increases; the Fe site is another matter. How this moment evolves with temperature as the Cr concentration is varied, is a complex question beyond the scope of this paper.

#### 3.2. Magnetic properties

[Fig. 4](#page-4-0) shows representative M-H characteristics for the (Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> alloy films investigated in this study. [Fig. 5](#page-5-0) compares the experimentally-determined  $M_s$  of the 2.5 and 11 nm films at 10 K and 300 K with the DFT calculations, which simulate bulk material at a temperature of 0 K. There is excellent agreement, especially for the 11 nm films at 10 K. The experimental observation that alloying with only 10% Cr reduces  $M_s$  by about 30% from that of the host  $\text{Ni}_{80}\text{Fe}_{20}$  material, suggests that the Cr is entering the Ni<sub>80</sub>Fe <sub>20</sub> antiferromagnetically.

The measured  $M_s$  of the 2.5 nm films at 300 K is consistently lower than that of the 11 nm films for each Cr alloy fraction. At 10 K this difference is smaller, and is negligible for films with more than 10% Cr. The smaller  $M_s$  for thinner (Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> alloy films can possibly result in part from a magnetic dead layer at the interfaces that arises from interdiffusion, the presence of strain, or reduced coordination number. By extrapolating the measured magnetic moment as a function of film thickness over the range of 1.5–11 nm, we determined an approximate magnetic dead layer thickness of 0.55 nm for the host  $N_{80}Fe_{20}$  material at T = 10 K, which decreases to 0.1 nm with the addition of 10% Cr. The reduced dead layer thickness with increasing Cr is not currently understood. The difference in  $M_s$  may also partly be due to a lower  $T_c$  for the 2.5 nm films, which would arise from a reduction of the



<span id="page-4-0"></span>

Fig. 4. Representative M-H loops taken of (Ni<sub>80</sub>Fe<sub>20</sub>)<sub>85</sub>Cr<sub>15</sub> films at two thicknesses (2.5 nm and 11 nm) and at two temperatures (10 K and 300 K).



Fig. 5. Data points are the experimentally measured quasistatic M<sub>s</sub> of the Nb/Ru/(Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub>/Ru/Nb films, at 10 K (left graph) and 300 K (right graph). The lines are the density functional theory (DFT) predictions, which model bulk material at 0 K. Note the relatively good agreement found between theory and experiment for the thicker 11 nm films measured at the lowest temperature of 10 K.

average exchange energy due to surface effects. This would help to explain why the reduced  $M_s$  for the 2.5 nm film is less pronounced at low temperatures, far below  $T_c$ . A lower  $T_c$  for the 2.5 nm films is also consistent with their lower  $M_s$  measured magnetodynamically at 300 K, since the  $M_s$  determined in this way does not depend on any assumptions about a magnetic dead layer. (See [Fig. 13](#page-8-0) and associated discussion below.)

There is a decreasing trend in both the experimentally measured  $T_c$  of the 11 nm films and the mean-field  $T_c$  calculation from the DFT, shown in [Fig. 6](#page-5-0). This trend indicates that the introduction of the antiferromagnetically oriented Cr weakens the exchange interactions, as expected. There is a relatively constant difference between DFT-predicted and measured  $T_c$  values. This discrepancy is attributed to the neglect of spin fluctuations and other dynamic effects, which are not taken into account in the DFT calculations

when using the Heisenberg model. Longitudinal spin fluctuations can, on average, bring spins closer together, increasing the exchange integral and thereby increasing  $T_c$ . In a situation like this, neglecting longitudinal spin fluctuations can cause an underestimate of  $T_c$  like the one seen here.

At room temperature, the 35% Cr films were paramagnetic for both thicknesses, while the 28% films were superparamagnetic for both thicknesses, as expected from the measured  $T_c$ .

[Fig. 7](#page-6-0) shows the measured coercivity  $H_c$  for the (Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> films at 10 K (right graph) and 300 K (left graph). A low  $H_c$  indicates good magnetically soft properties for  $Ni_{80}Fe_{20}$ -based thin films. The coercivity values in [Figs. 7 and 8](#page-6-0) that fall near or below 0.2 Oe are not believed to be reliable, as we observe that the coercivity determinations of such samples typically varied from 0.0 to 0.2 Oe from measurement to measurement.

<span id="page-5-0"></span>

Fig. 6. The experimentally-measured Curie temperature  $T_c$  in 11 nm  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  versus Cr continent,%Cr, compared with values simulated using DFT. Neglect of longitudinal spin fluctuations in the simulation are the likeliest cause of the discrepancy with the experimental results.

We attribute this to a combination of the limited instrumentation accuracy and the irreproducible nature of the dynamics of small coercivity magnetic films.

At 10 K, the addition of up to  $\sim$  15% Cr into Ni<sub>80</sub>Fe<sub>20</sub> does not significantly alter  $H_c$ , but for larger percentage of Cr, the  $H_c$  begins to increase. This increase in  $H_c$  is due to increased domain-wall pinning in the film and is characteristic of inhomogeneous and magnetically defective material. Such an increase would result in degraded switching behavior in devices, such as MRAM. X-ray diffraction measurements in both our study and that of Specht et al. [\[22\]](#page-10-0) show that Cr enters the lattice without forming significant amounts of secondary phases or interstitial defects for the alloy compositions studied here. Thus, we conclude that the inhomogeneity in the substitutional Cr content through the film is responsible for the observed increase in the  $H_c$  from domain wall pinning. At 300 K, the thermal activation reduces the amount of applied field required to effect domain wall motion, thereby reducing the  $H_c$ . The downward trend in  $H_{ce}$  for increasing Cr content in the 2.5 nm films at  $T = 300$  K is likely related to the sharp decrease in  $M_s$  as T<sub>c</sub> approaches 300 K. The H<sub>c</sub> of the 2.5 nm films is significantly larger than  $H_c$  for the 11 nm films at 10 K, which can be caused by defects from surface/interface roughness and or lattice strain. However, the hard-axis  $H_c$  is similar for both thicknesses at 300 K, which indicates that the energy barriers related to defects are much smaller than the thermal energy of 26 meV.

The easy-axis remanent squareness  $Sq_e$  and hard-axis remanent squareness  $Sq_h$  measured for the  $(Ni_{80}Fe_{20})_{100-x}Cr_x$  films are shown in [Fig. 8](#page-4-0). Ideally, for soft  $Ni_{80}Fe_{20}$  with induced uniaxial  $H_k$ , the easy-axis squareness of  $\approx$ 1 and the hard-axis squareness of  $\approx$ 0. For the 11 nm samples, the easy-axis squareness and hard-axis squareness are close to ideal for almost all samples measured -- the only deviation is an increase in hard-axis squareness of over 0.2 at T = 10 K and a Cr content of over 10%, which correlates with the increase in the hard-axis coercivity observed for these samples. For the 2.5 nm samples, the easy-axis squareness at 300 K drops significantly with high Cr content. For the 2.5 nm samples, at 10 K, the easy-axis squareness decreases slightly and the hard-axis squareness increases more significantly with increasing Cr content. This degradation correlates with the increase in  $H_c$ observed for these samples at 10 K and indicates increased magnetic defectivity in the thinner films, as discussed previously.

The hard axis uniaxial anisotropy  $H_k$  measured for the  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  films is shown in [Fig. 9](#page-6-0). Values for H<sub>k</sub> were obtained from the hard axis hysteresis loops by fitting the region between negative magnetic saturation and positive magnetic saturation to a straight line. Dividing  $M_s$  by the slope of this line gives the field needed to saturate the film, i.e.  $H_k$ . For most of the films,  $H_k$  was reduced by the addition of Cr, though  $H_k$  for the 11 nm film with Cr 20% increased slightly. The increased  $H_k$  at 10 K for the 2.5 nm films with large Cr content is likely an artifact of the large  $H_c$  for these films, and does not reflect a true increased uniaxial anisotropy. The decrease in  $H_k$  with increasing Cr content is a result of the increasing amount of disorder of the film, particularly



Fig. 7. Dependence of easy-axis coercivity H<sub>ce</sub> and hard-axis coercivity H<sub>ch</sub> on Cr content of the Nb/Ru/(Ni<sub>80</sub>Fe 20)100-xCrx /Ru/Nb films. Note the H<sub>c</sub> increase for larger Cr content observed at 10 K is absent at 300 K, likely due to increased thermal fluctuations and the relatively slow time scale of the measurement.

<span id="page-6-0"></span>

Fig. 8. Cr content dependence of easy- and hard-axis remnant squareness,  $Sq = M_r/M_s$ , of the Nb/Ru/(Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> /Ru/Nb films. Absence of typical anisotropy at 300 K in 2.5 nm thick samples with 5% Cr and 10% Cr resulted in high Sq-h in these samples.



Fig. 9. dependence of the quasistatic anisotropy field H<sub>k</sub> on the Cr content in the Nb/Ru/(Ni<sub>80</sub>Fe<sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> /Ru/Nb films at 300 K (left graph) and 10 K (right graph) and for different thickness of film (Crosses = 11 nm, Circles = 2.5 nm). The estimated measurement accuracy for the quasi-static Hk values is estimated to be ± 0.5 Oe.

the breaking up of the directional pair ordering of the alloy's Ni and Fe atoms. Other studies have reported an increase in anisotropy at Cr contents over 40% and attributed it to enhanced exchange bias [\[29\]](#page-10-0). This study did not investigate alloys with high enough Cr content to see this effect.

The magnetodynamic properties of the  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  films were measured at room temperature using a custom built PIMM. The inductive electrical signals  $v(t)$  from the films were fit to an exponentially damped sinusoid -- a function which accurately describes the behavior of a decaying ferromagnetic resonance produced by a step-excitation in magnetic field [\[26\].](#page-10-0) Specifically, the signal is fit to the equation

$$
v(t) = v_0 e^{-(t-t_0)/\tau} \cos(2\theta f_p(t-t_0) + \phi_o) \mu(t-t_0)
$$

where  $\tau$  is the resonance decay time, and  $f_p$  the precessional frequency. The Landau-Lifshitz damping parameter  $\lambda$ , is related to  $\tau$ as  $\lambda = 2/\tau$  in SI units, or  $\lambda_{cgs} = 2/(4\pi\tau)$  in CGS units.  $f_p$  is used to calculate Ms, but several  $f_p$  values from a range of bias fields are required (see below). The other fit parameters--  $v_0$ ,  $t_0$ , and  $\varphi_0$ -- are not used to calculate any material properties. The damped-sinusoid fit is valid assuming a soft material is being measured (i.e.  $M_s \gg H_k$ ) and that the deflection of the mean-field magnetization with respect to equilibrium is small.  $M_s \gg H_k$  is always the case for the materials in this study, and a small angle of deflection can be assured by beginning the fit shortly after the start of the inductive signal. [Fig. 10](#page-7-0) shows two examples of PIMM signal fits. For a more detailed explanation of the model used to analyze PIMM signals, see Ref. [\[26\]](#page-10-0). [Fig. 11](#page-7-0) shows the  $\tau$  and  $\lambda$  cgs as a function of

<span id="page-7-0"></span>

Fig. 10. Time-resolved inductive signals measured using PIMM (grey line), and the damped sinusoid fit used to extract  $\tau$  and  $f_p$  at a given bias field (solid black line). The envelope of the sinusoid, which is determines the magnitude of the damping parameter, is shown as well (dotted black line). The vertical dotted line indicates the beginning of where data is taken for the damped sinusoid fit. This data was taken at room temperature.



Fig. 11. Magnetodynamic damping parameter  $\lambda_{\text{cgs}}$  (right axis) and the FMR decay time  $\tau$  (left axis) versus easy axis bias field H<sub>b</sub> for a 11 nm and 2.5 nm  $(Ni_{80}Fe_{20})_{95}Cr_5$  film from fits of exponentially-damped sinusoids to the PIMM data. The increase in  $\lambda$  cgs at low bias field is due to extrinsic contributions to damping from magnetic dispersion in  $H_k$ . At larger bias fields, the magnetization is more uniformly aligned and a field-independent damping is obtained. Error bars were determined from constant  $\chi^2$  boundaries of the fit to the inductive waveform. There are no data points for the 2.5 nm film at low bias fields due to the absence of a detectable inductive signal.

easy axis bias field H<sub>b</sub> for an 11 nm and a 2.5 nm ( $\text{Ni}_{80}\text{Fe}_{20}\text{)}_{95}\text{Cr}_{5}$ film. Films having different Cr content or thickness behaved similarly. The Landau-Lifshitz damping parameter  $\lambda$ , is related to  $\tau$  as  $\lambda = 2/\tau$  in SI units, or  $\lambda_{\text{cgs}} = 2/(4\pi\tau)$  in CGS units [\[26\]](#page-10-0). As shown, the value of  $\tau$ (or  $\lambda$ ) increases (decreases) strongly with increasing magnitude of the bias field,  $H<sub>b</sub>$ . When little or no bias field is applied,  $\lambda_{\text{cgs}}$  is much larger due to extrinsic contributions arising from nonuniform magnetization caused by magnetic dispersion in Hk. As the bias field is increased to over 20 Oe, the magnetization is forced to become more uniform, and  $\lambda$  converges to a reduced damping that is approximately field-independent and closer to an intrinsic value for this particular alloy. We averaged the  $\tau$  and  $\lambda$  data for bias fields from 25 Oe to 75 Oe for each sample and show the results in [Fig. 12](#page-8-0). While  $\lambda$  only slightly increases with increasing Cr content, a large increase occurs for the thinner 2.5 nm films.

What is interesting to note in these measurements is that the high field damping  $\lambda$  does not appear to change by a significant amount with the increase in Cr content, in contrast to the quasistatic switching properties. A previous study of the damping parameter in transition metal-doped  $Ni_{80}Fe_{20}$  systems [\[23\]](#page-10-0) also found that the presence of Cr does not significantly change  $\lambda$  until the Cr content is  $\sim$ 25%, after which  $\lambda$  begins to increase. Adding transition metal dopants to  $Ni_{80}Fe_{20}$  typically increases  $\lambda$  primarily through an increase in spin-orbit coupling. Since Cr is similar in atomic number to the host elements, Ni and Fe, and thus has similar spin–orbit coupling, the presence of small amounts of Cr ( $\langle \sim 20\%$ ) does not cause a significant increase in  $\lambda$ . In contrast, the damping parameter  $\lambda$  depends strongly on the film thickness. The decrease in  $\tau$  from  $\sim$ 1.1 ns to  $\sim$ 0.6 ns (or increase in  $\lambda$  from  $\sim$ 150 MHz to  $\sim$ 250 MHz) could be due to an increase in the relative density of inhomogeneous regions that impede magnetization rotation with decreasing film thickness. The inhomogeneity can originate from disorder at interfaces due to interdiffusion, surface roughness, and possibly lattice strain. An increase in material inhomogeneity is also consistent with the larger hard-axis coercivity observed for the thinner 2.5 nm films at 10 K. Low temperature measurements often correlate better with high speed magnetic properties, since both have reduced effects of thermal activation on the magnetic properties.

However, it is also possible some part of the increase in  $\lambda$  is caused by spin-orbit coupling from the  $Ru/Ni_{80}Fe_{20}$ interface now acting on a smaller magnetic volume (sometimes referred to as a spin pumping effect). We found comparable  $\lambda$  for 2.5 nm thick  $Ni_{80}$ Fe <sub>20</sub> films in direct contact with Nb, but Nb and Ru have similar atomic number. Determining the effect of interfacial spin-orbit coupling on  $\lambda$  would require additional samples to be evaluated and is beyond the scope of this study.

The  $M_s$  and  $H_k$  values (shown in [Fig. 13\)](#page-8-0) were obtained by fitting the FMR precessional frequencies  $f<sub>p</sub>$  vs. applied bias field  $H<sub>b</sub>$  with the Kittel equation:

$$
{f}_p=|\gamma|\sqrt{M_s(H_k+H_b)}
$$

where  $\gamma$  is the gyromagnetic ratio [\[26\].](#page-10-0) The "dynamical" M<sub>s</sub> and H<sub>k</sub> values deduced from the Kittel equation fits differ from those measured using quasistatic methods. The dynamic  $M_s$  is approximately 10% larger than that determined using VSM at 300 K. The cause of the difference is not currently understood, though the dynamic  $M_s$  value of  $\approx 875$  emu/cm<sup>3</sup> for  $Ni_{80}Fe_{20}$  is slightly larger than expected. The relatively lower dynamic  $M_s$  for 2.5 nm films compared to 11 nm is consistent with the  $M_s$  results determined using VSM at 300 K. The value of  $M_s$  determined by PIMM depends on field calibration of the bias field coils, the time calibration of the oscilloscope, and includes contributions from any perpendicular anisotropy (which is typically near 0 for  $Ni_{80}Fe_{20}/Ru$  interfaces). Thus we can reasonably conclude the lower  $M_s$  for thinner films is real, and not an artifact of using an incorrect volume or a magnetic dead layer. We attribute the lower  $M_s$  to most likely originate from a lower  $T_c$  for thinner films.

The  $H_k$  for the 11 nm films exhibits a small decrease with increasing Cr percentage, and then increases at the large Cr content, similar to what was observed for  $H_k$  as measured quasistatically by VSM. Of particular interest is the negative dynamic  $H_k$ values for the 2.5 nm films. This means that the precession frequency has been reduced uniformly over the range of applied bias field  $H<sub>b</sub>$  due to effects associated with the reduced film thickness. This effect appears to be unrelated to the addition of Cr, as the difference between dynamic  $H_k$  in the 11 nm and 2.5 nm films is roughly constant over the range of Cr levels. The main cause is

<span id="page-8-0"></span>

Fig. 12. Magnetodynamic damping parameter  $\lambda_{\text{cgs}}$  (right axis) and FMR decay time  $\tau$  (left axis) in (Ni<sub>80</sub>Fe<sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> versus Cr content (%Cr) for 11 nm (crosses) and 2.5 nm (circles) films from fits of exponentially-damped sinusoids to the PIMM data. The values shown at the points are averages of bias fields from 25 Oe to 75 Oe. The bars around each data point show the range of the damping parameter over the measured bias fields. The addition of Cr only slightly increased  $\lambda_{\rm cgs}$ , but thinner 2.5 nm (Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> films showed a large increase in  $\lambda$  cgs.



Fig. 13. Dynamic M<sub>s</sub> and Dynamic H<sub>k</sub> versus Cr content dependence of the of the Nb/Ru/(Ni<sub>80</sub>Fe <sub>20</sub>)<sub>100-x</sub>Cr<sub>x</sub> /Ru/Nb films, determined using fits of the Kittel FMR relation to the PIMM data. The lower M<sub>s</sub> for the 2.5 nm films is attributed to a lower T<sub>c</sub>, and is consistent with the M<sub>s</sub> determined using VSM [\(Fig. 5\)](#page-5-0). The negative dynamic H<sub>k</sub> for the 2.5 nm films is attributed to increased magnetic dispersion creating a demagnetizing field opposing H<sub>b</sub>.

most likely increased magnetic dispersion in  $H_k$  of the 2.5 nm film due to increased material inhomogeneity, as described previously. If the magnetization is spatially non-uniform, then a demagnetizing field will be generated in the film that can oppose the applied bias field  $H<sub>b</sub>$ , thereby reducing the precession frequency. This effect is similar to the observed reduction in the precession frequency versus wavelength relationship for backward volume magnetostatic spin waves [\[30\]](#page-10-0). Assuming the actual intrinsic  $H_k$  for the 2.5 nm film is the same as the 11 nm film, the dispersion-induced demagnetizing field is approximately  $\sim$ 10–15 Oe. Aside from this offset, the variations in dynamic  $H_k$  with Cr content are in qualitative agreement with the variations seen in the quasistatic  $H_k$ .

#### 3.3. Electrical properties

Using the Sommerfeld model, as outlined by Ashcroft and Mermin [\[31\]](#page-10-0), one can use the measured resistivity and lattice constant to determine a reasonable estimate of the majority mean free path in our  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  alloys. Fig. 14 compares the inferred majority mean free path, which is found to be much smaller than



Fig. 14. Comparison of majority carrier mean free path calculated using the Sommerfeld model (using measured resistivity and lattice constant) with values predicted from DFT simulation.

the grain size, with the predictions from the density functional calculations within the coherent potential approximation. Good agreement is obtained at higher levels of Cr content, but not at the lower levels. This is somewhat surprising, given that earlier studies have found that alloy scattering dominates the scattering process in  $Nis<sub>0</sub>Fe<sub>20</sub>$  and that the density functional calculations with the use of the coherent potential approximation give an excellent agreement with the scattering parameters measured with angle resolved photoemission [\[32\]](#page-10-0) (See Fig. 15).

The theoretical results in Fig. 16 indicate that alloying with Cr does not significantly alter the overall band structure, but does introduce alloy scattering, almost entirely for the majority carriers. This explains why the resistivity increases markedly when alloying with Cr. It is interesting that in contrast to this, as we reported before  $[19]$ , alloying Ni<sub>80</sub>Fe<sub>20</sub> with Cu only moderately increased the scattering of the majority band in alloys, while the minority band is scattered strongly. Since the majority band carries most of the current,  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  alloy materials with the same



Fig. 15. Cr content dependence of the mean free path for majority and minority carriers in  $(Ni_{80}Fe_{20})_{100-x}Cr_x$ . These values were obtained using DFT simulations. While the majority mean free path reduces drastically with increasing Cr content, the minority mean free path does not change significantly.



Fig. 16. The potential parameter, C, representing the d-band energy centers for Ni, Fe, and Cr majority and minority spins. These values were obtained using DFT simulations. The minority spin levels show large mismatch almost independent of the Cr concentration, in contrast to the majority spins, where the mismatch being small initially increases significantly with the addition of Cr; which leads to a small change in scattering for minority spins and a large increase in scattering for majority spins.

fraction of alloying agent have a much lower resistance than other Ni-Fe alloys [\[33\].](#page-10-0)

We will show that a simplified model derived from the DFT analysis using potential parameters can provide a straightforward way to understand the way alloying agents affect both the minority and majority scattering. The methodology used in this formal-ism is fully described in Ref. [\[19\],](#page-10-0) and the references therein. In the model, two dominant parameters,  $C$  and $\Delta$ , are derived from the DFT analysis. The band parameter C is the band center of a partial wave and is comparable to the tight-binding on-site energy.  $\Delta$ is the parameter that describes the bandwidth. The mismatch in C between each of the alloy constituents (see Fig. 16) represents the spin-dependent scattering potential and dominates the transport process when the differences are on the order of a half a volt or more. Under such conditions, other sources of scattering such as spin-orbit coupling are much less influential. This conclusion is further supported by the observation that the spin-orbit corrections to the Hamiltonian are small in magnitude and to a good approximation we can consider the spin channels as independent.

The average value  $(C \uparrow + C \downarrow)/2$ , where the up/down arrows represent the majority/minority channels, is almost independent of the local magnetic moment, m, and is more stable in energy for higher atomic numbers along the rows of the periodic table. The splitting between  $C \uparrow$  and  $C \downarrow$  depends primarily on the local magnetic moment of the particular element in the solid. Fig. 16 summarizes the values of  $C \uparrow$  and  $C \downarrow$  for  $Cr_{1-x}(Ni_{80}Fe_{20})_x$  alloys. The average value on a site,  $(C \uparrow + C \downarrow)/2$  scales as expected in the order Cr, Fe, Ni. The spin splitting on the Fe site  $(C \uparrow -C \downarrow)$  is largest among the elements and is not strongly dependent on the alloy fraction, at least for  $Ni<sub>80</sub>Fe<sub>20</sub> content above 80%. As is found in general in most solids,$ Fe has a large local moment. Cr too has a large moment, although its moment is more strongly quenched by the presence of enhanced levels of Cr. In contrast to Fe and Cr, Ni's local moment (i.e.  $C \uparrow -C \downarrow$ ) is smaller than the other elements in this alloy.

Fig. 16 shows that the Cr majority potential falls significantly above the Fe and Ni, particularly for concentrations above about 10% Cr. This indicates that the majority spin channel would be expected to be strongly scattered with the addition of Cr into the Ni<sub>80</sub>Fe <sub>20</sub> lattice as the mismatch for majority channel (especially between Ni and Cr) increases significantly. In contrast, it can also be seen from the figure that the mismatch for minority spin (even though quite large even at the low concentration of Cr) remains almost constant with the change in Cr-concentration. Thus, we would expect that the minority scattering to be largely independent of Cr content for these alloys of interest, as is borne out in the calculations.

#### 4. Conclusion

This study investigated the prospects of  $(Ni_{80}Fe_{20})_{100-x}Cr_{x}$  alloys as a potentially useful low  $M_s$  material at both room and cryogenic temperatures. The magnetic (quasistatic and magnetodynamic), transport, and structural properties of a range of  $(Ni_{80}Fe_{20})_{100-}$  $_{x}Cr_{x}$  alloys at several film thicknesses were measured. We found for a wide range of Cr up to  $\sim$ 15%, the magnetic properties were of sufficient quality that these alloys could be useful in magnetic device technologies. One example is a  $(Ni_{80}Fe_{20})_{85}Cr_{15}$  alloy that has very desirable properties, including at  $4 K a$  reduced  $M<sub>s</sub>$  of  $\approx$ 500 emu/cm<sup>3</sup>, an H<sub>c</sub> of  $\approx$ 4 Oe, an H<sub>k</sub> of  $\approx$ 1 Oe, and remanent squareness Sq of  $\approx 0.8$ .

#### Acknowledgements

This work was supported by IARPA through Contract N66001- 12-C-2020. MvS was supported by EPSRC CCP9 Flagship Project <span id="page-10-0"></span>No. EP/M011631/1. The use of facilities in the LeRoy Eyring Center for Solid State Science at Arizona State University is acknowledged.

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